

CONSTRAINING DARK MATTER with ASTEROSEISMOLOGY



Jordi Casanellas

in coll. with

Ilídio Lopes: Casanellas J. & Lopes I., ApJL 765 (2013) arXiv: 1212.2985

Isa M. Brandão: Casanellas J. & Brandão I., in preparation



Max-Planck-Institut
für Gravitationsphysik
(Albert-Einstein-Institut)

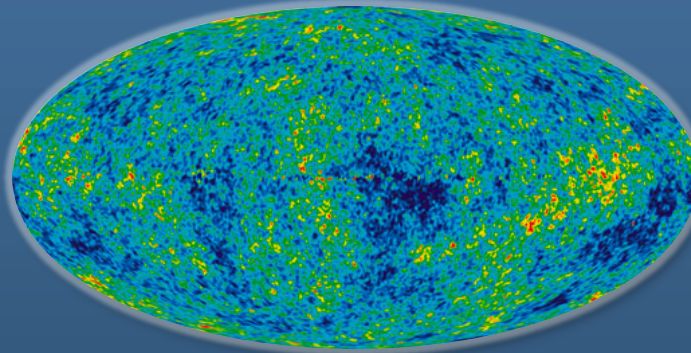
Unterstützt von / Supported by



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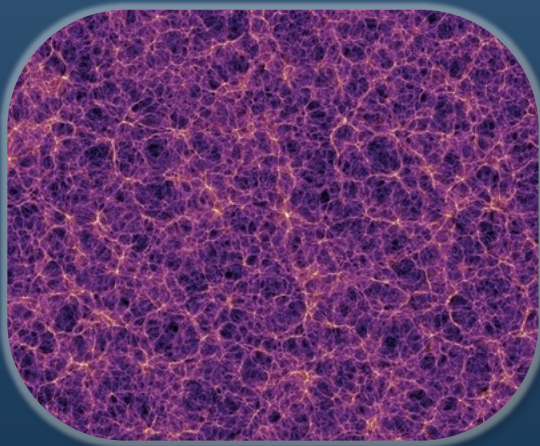
The Space Photometry Revolution, Toulouse 2014

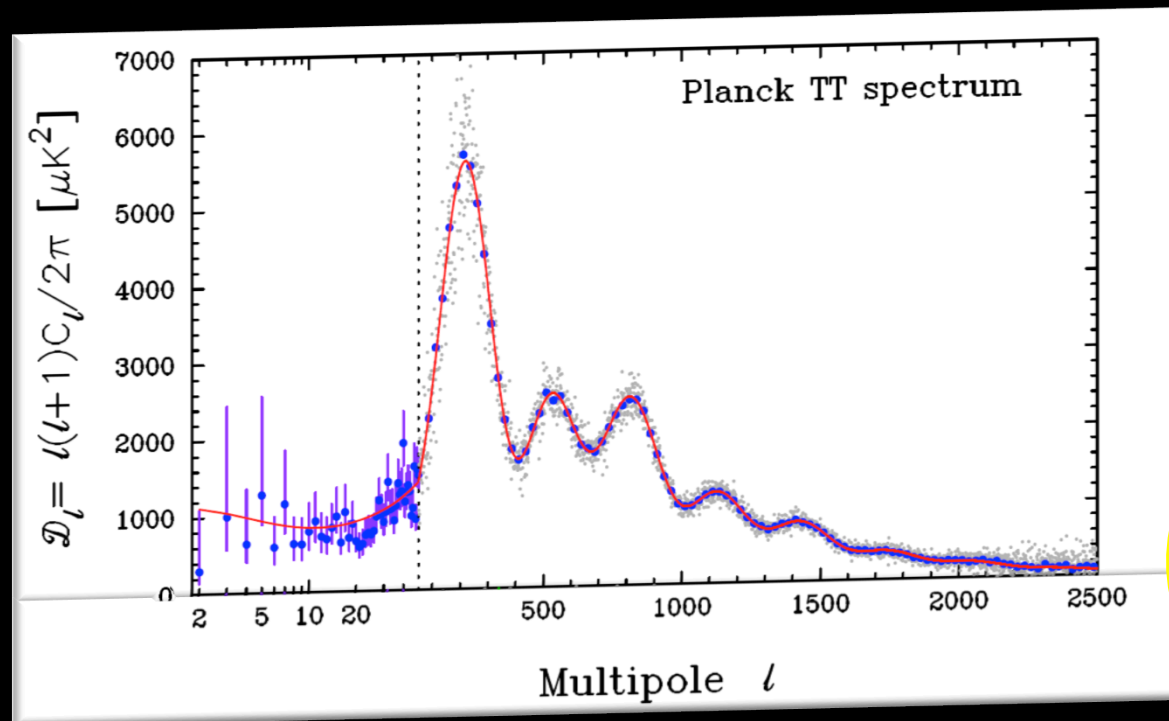
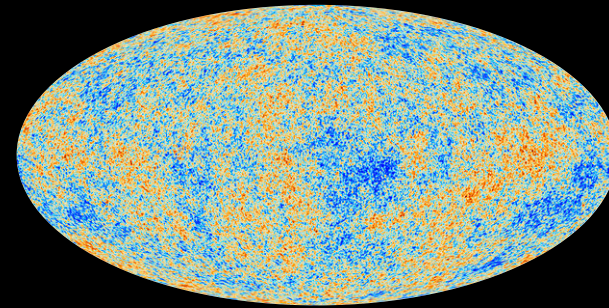
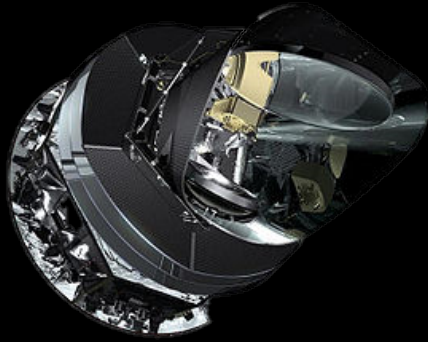
Dark Matter??



~ **80%** of all the matter exists
in an **unknown form**

- Massive
- Abundant
- Stable
- Weakly interacting with photons (neutral) and baryons



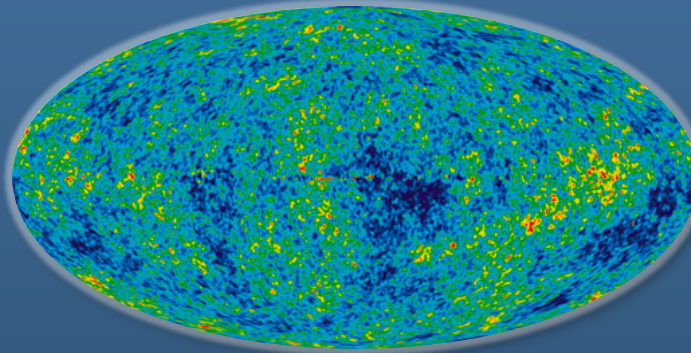


$$\Omega_m = 0.315$$

$$\Omega_b = 0.049$$

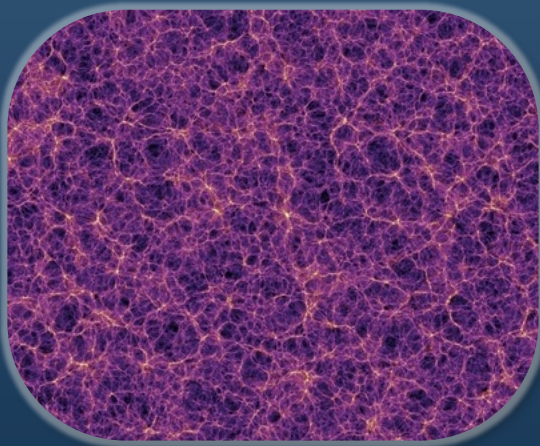
[PLANCK coll., arXiv:1303.5076 (2013)]

Dark Matter??

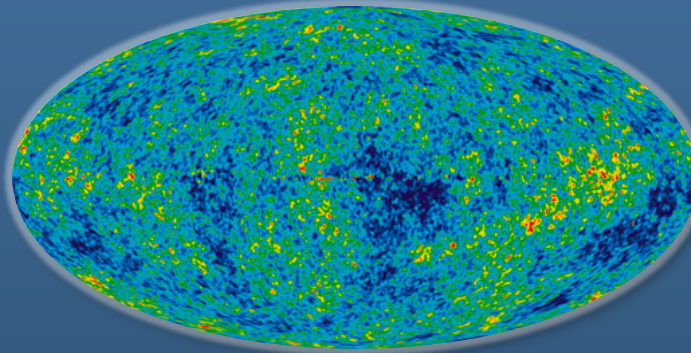


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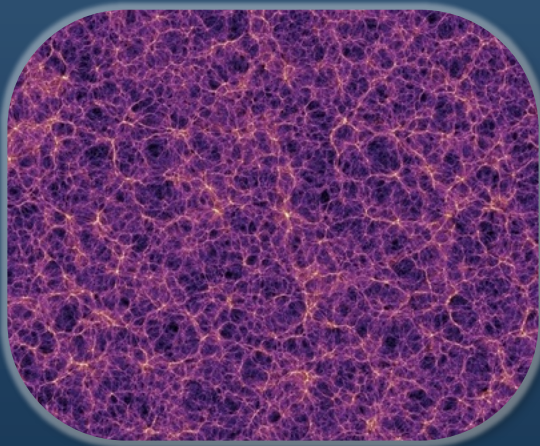
- Massive
- Abundant
- Stable
- Weakly interacting with photons (neutral) and baryons
- Non baryonic



Dark Matter??

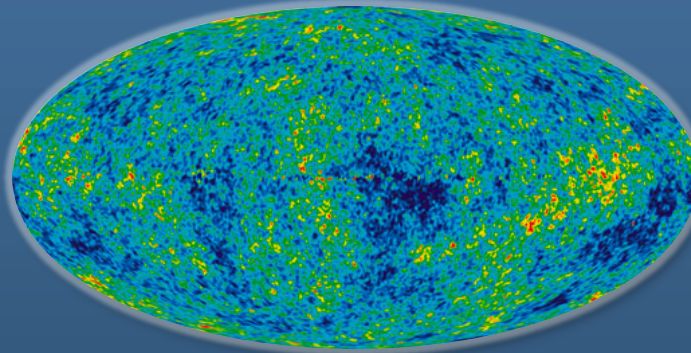


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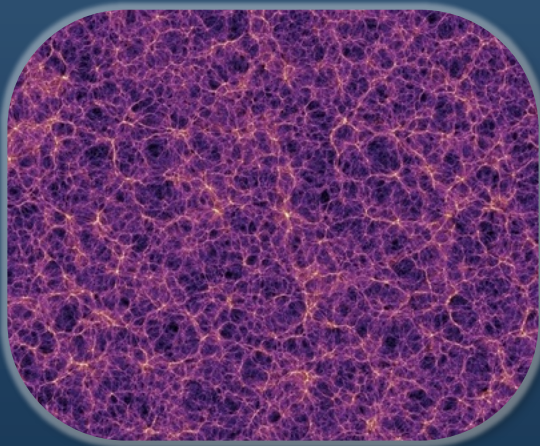


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- Cold (very non-relativistic)

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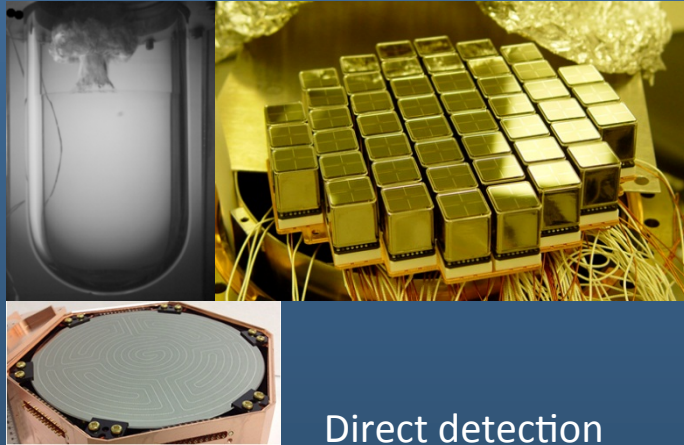


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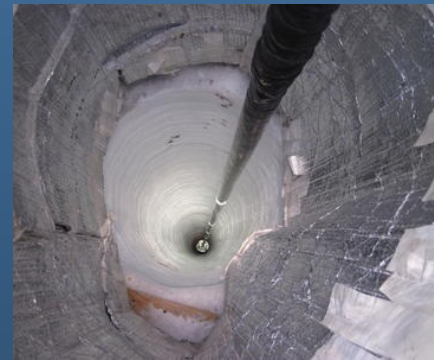
→ **WIMPs !**

axions,
sterile neutrinos,
gravitinos ...

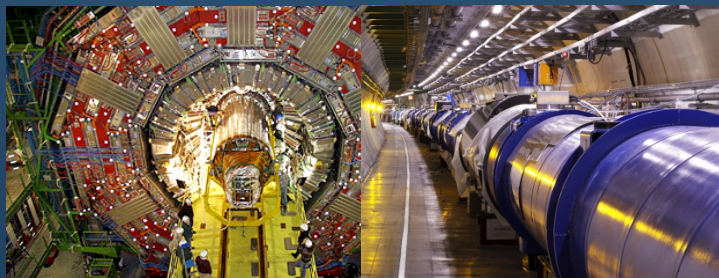
Dark Matter searches



Direct detection



Indirect detection



Colliders

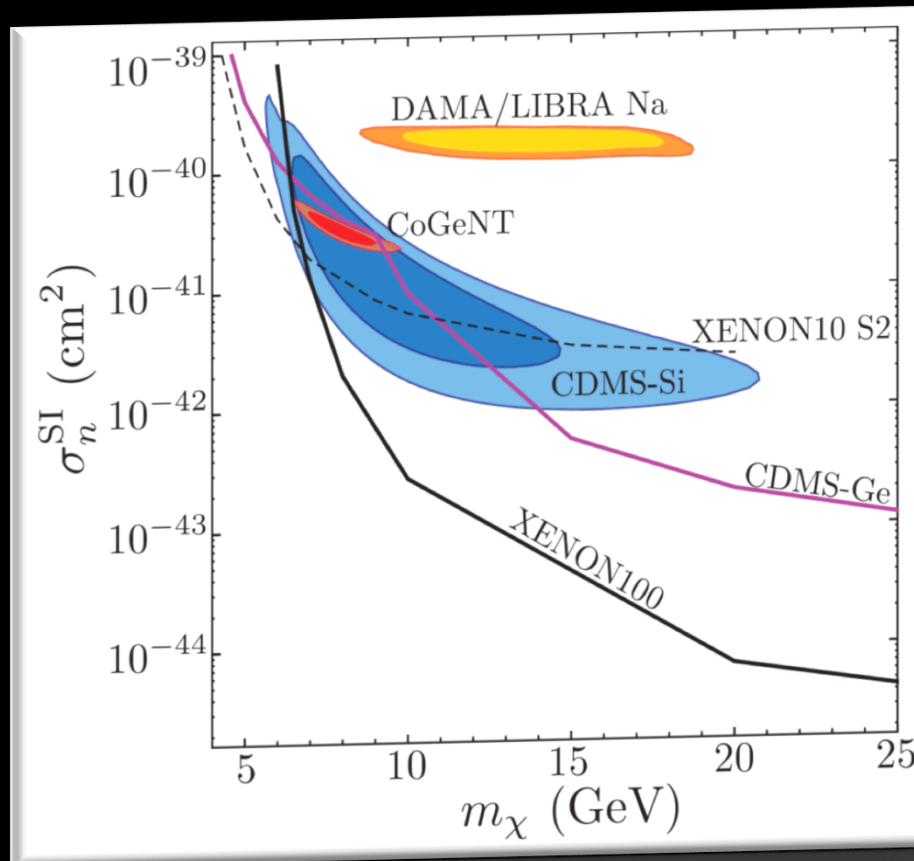


Astrophysical probes
(**STARS**)

Detection of Low-mass WIMPs ??

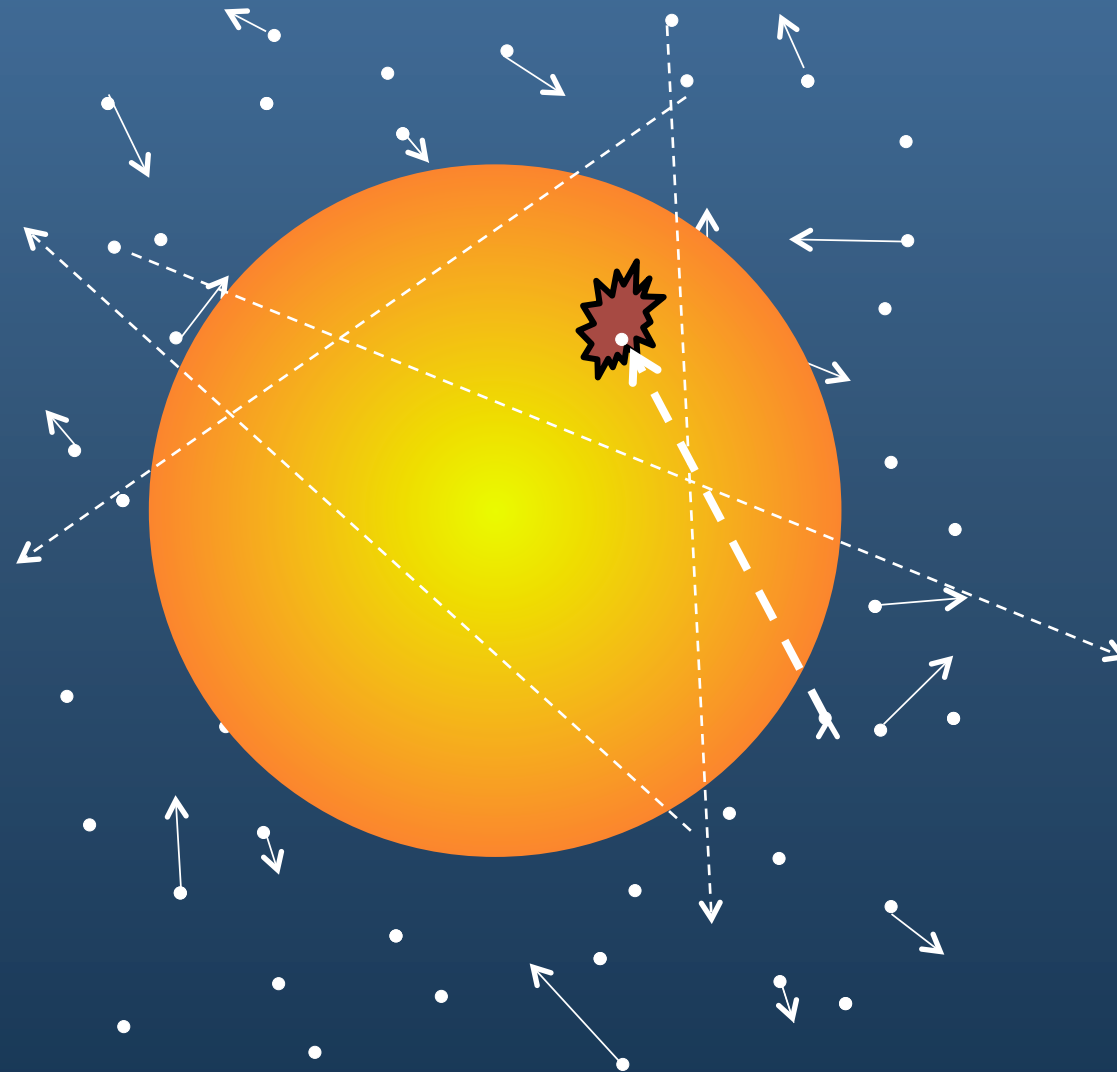
DAMA, CoGeNT, CRESST,
CDMS

Tension with null
results of
XENON100,
EDELWEISS

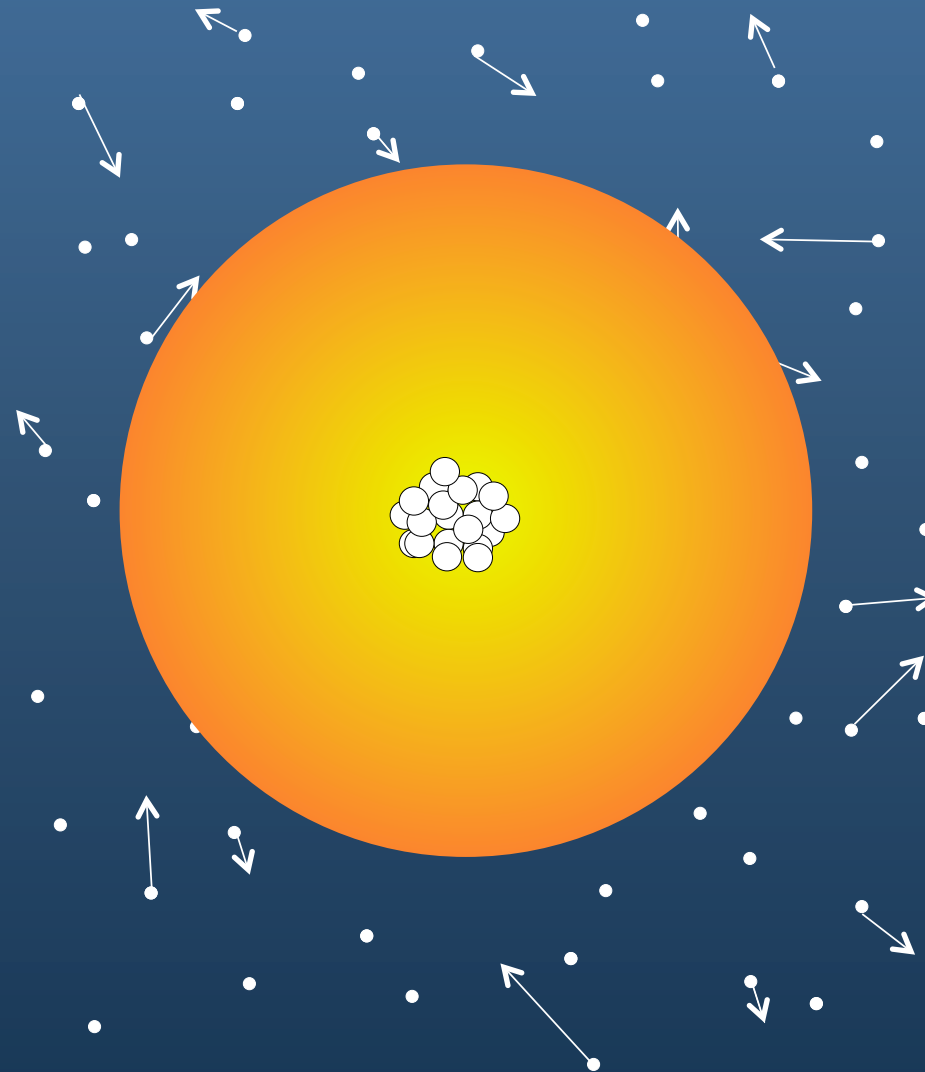


[Buckley M. & Lippincott W. H., Phys. Rev. D 88 (2013)]

Impact of Dark Matter on stars



Impact of Dark Matter on stars



DM Capture [Gould, ApJ 321 (1987)]

Jordi Casanellas, Toulouse 2014

Impact of Dark Matter on stars



DM Capture [Gould, ApJ 321 (1987)] + DM energy transport [Gould & Raffelt ApJ 352 (1990)]

Jordi Casanellas, Toulouse 2014

Impact of asymmetric Dark Matter on stars



DM Capture [Gould, ApJ 321 (1987)] + DM energy transport [Gould & Raffelt ApJ 352 (1990)]

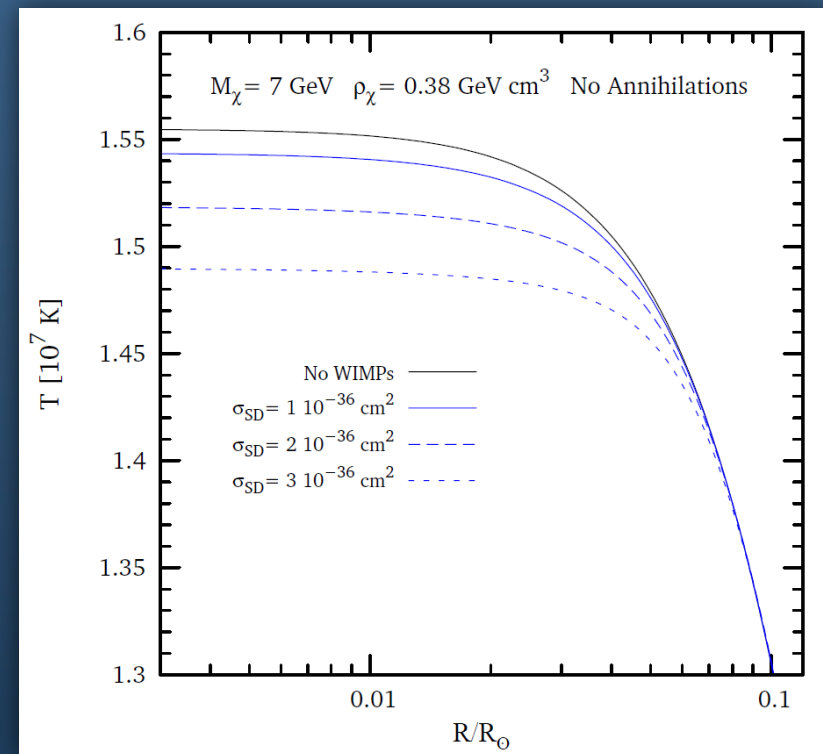
Impact of asymmetric Dark Matter on stars



DM energy transport
[Gould & Raffelt ApJ 352 (1990)]

Reduction central temperature

SUN: [Spergel and Press, ApJ 294 (1985)
Lopes, Bertone & Silk, MNRAS 337 (2002)...]

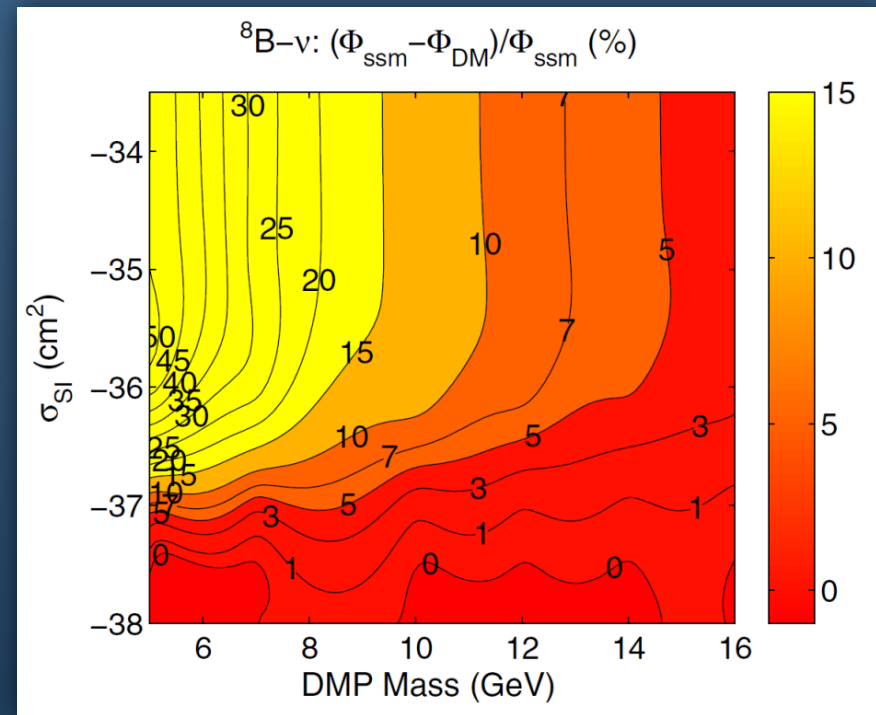
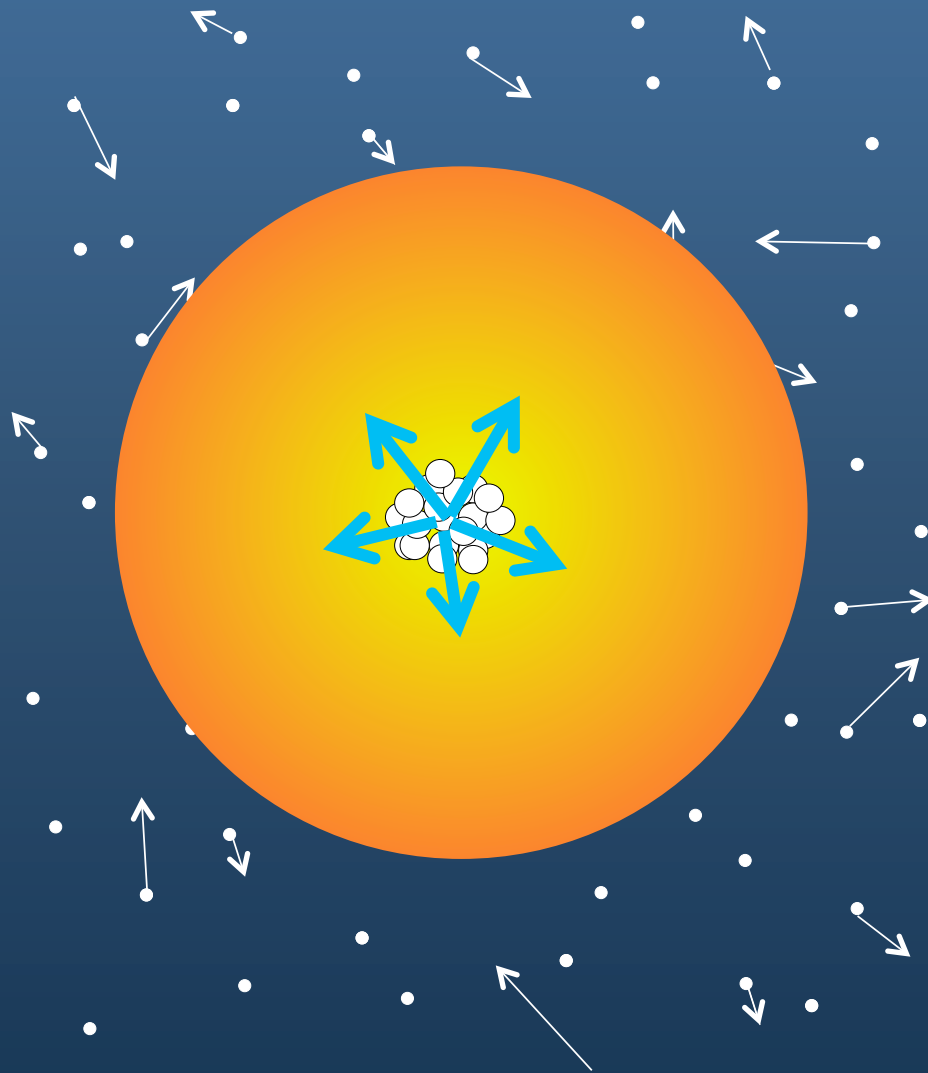


[Taoso *et al.* Phys. Rev. D 82 (2010)]

Impact of asymmetric Dark Matter on stars

Reduction central temperature

SUN: solar neutrinos, helioseismology



[Lopes & Silk, ApJL 752 (2012), Science (2012)]

Impact of asymmetric Dark Matter on stars

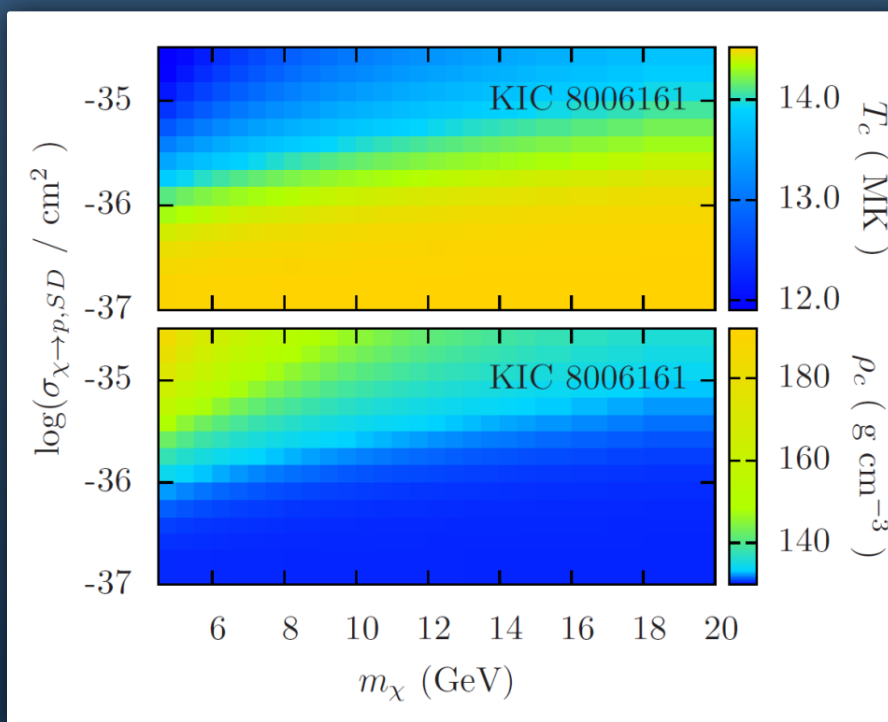


Reduction central temperature

SUN: solar neutrinos, helioseismology

WHY OTHER STARS ?

- $M_{\star} \downarrow \Rightarrow$ stronger DM impact



[Casanellas & Lopes , ApJL 765 (2013)]

How can asteroseismology constrain Dark Matter?



Constraining asym Dark Matter with asteroseismology

- Modelling of **α Cen B**
 $\Rightarrow M_{\star} \downarrow$, closest, binary

[Casanellas & Lopes, ApJL 765 (2013)]

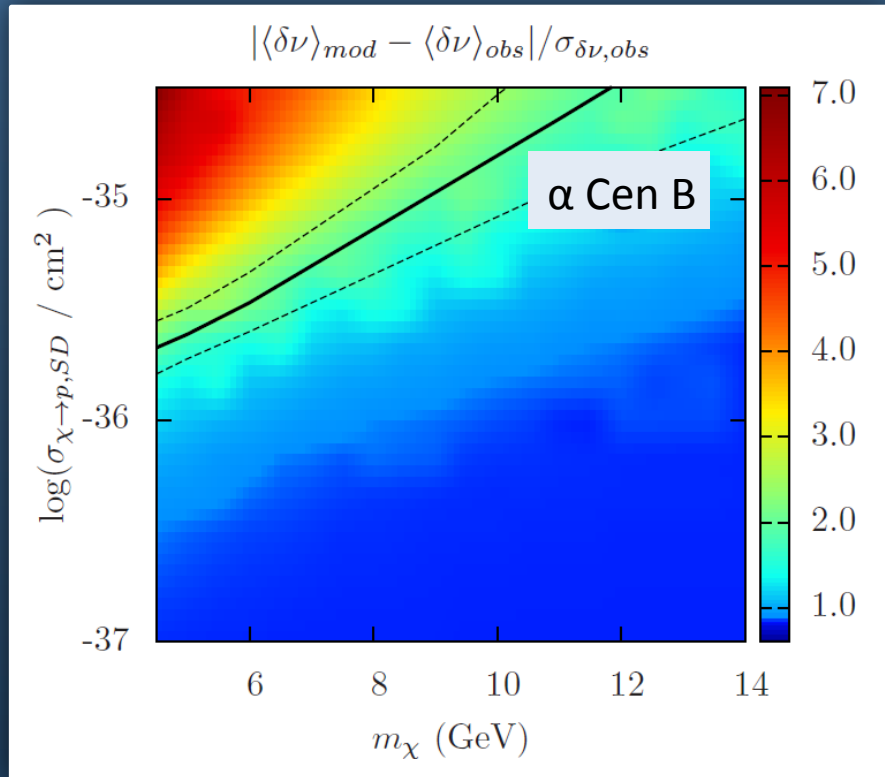
Asymmetric DM candidates with

$m_{\chi} = 6 \text{ GeV}$ and

$\sigma_{\chi, SD} \geq 3 \cdot 10^{-36} \text{ cm}^2$

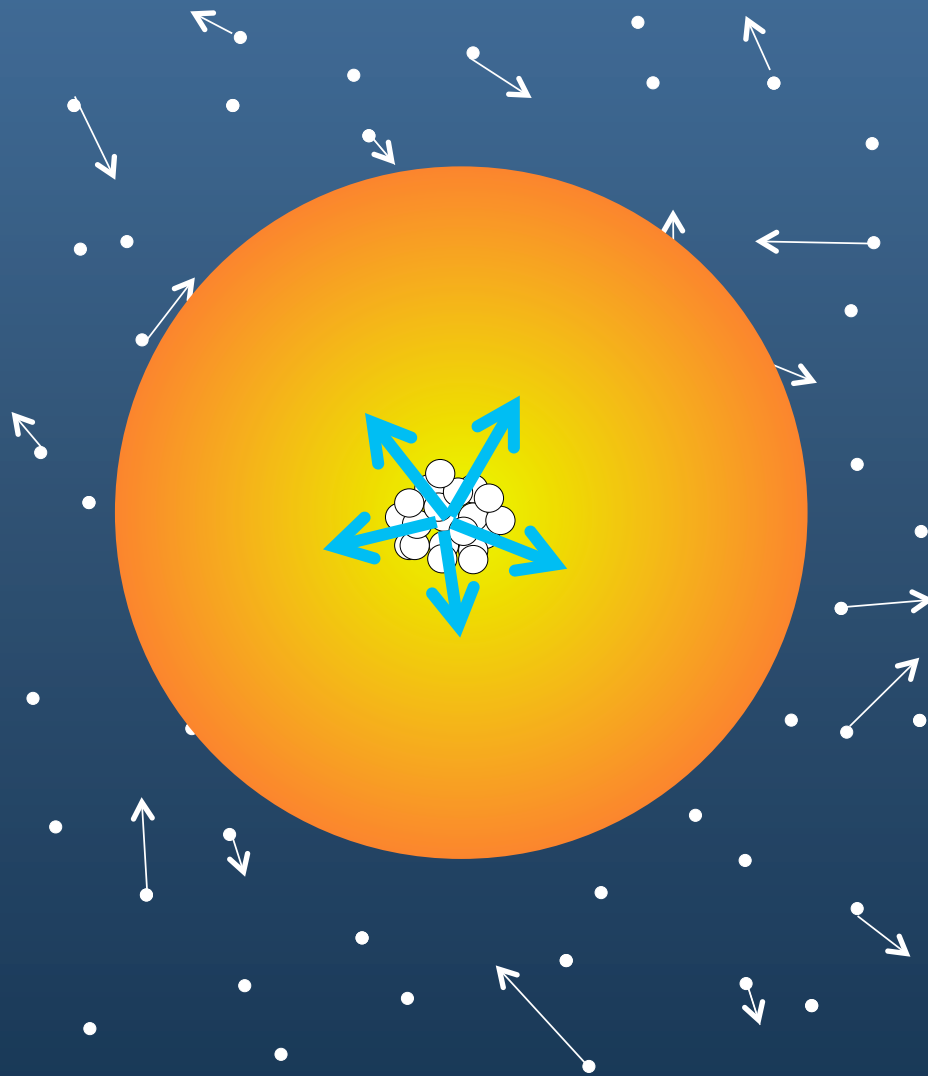
excluded at 95% confidence level.

$$\delta \nu_{n,l} = \nu_{n,l} - \nu_{n-1,l+2},$$



Star	M ($M_{\odot}$)	R ($R_{\odot}$)	L ($L_{\odot}$)	T_{eff} (K)	$(Z/X)_s$	$\langle \Delta \nu_{n,0} \rangle^a$ (μHz)	$\langle \delta \nu_{02} \rangle^a$ (μHz)
α Cen B							
Observ. [24, 25]	0.934 ± 0.006	0.863 ± 0.005	0.50 ± 0.02	5260 ± 50	0.032 ± 0.002	161.85 ± 0.74	10.94 ± 0.84
Stand. mod./DM mod. ^c	0.934	0.868	0.51	5245/5230	0.031	162.56/162.45	10.23/8.95

Impact of asymmetric Dark Matter on stars



Reduction central temperature

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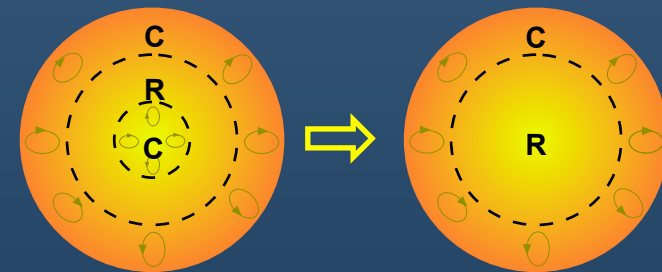
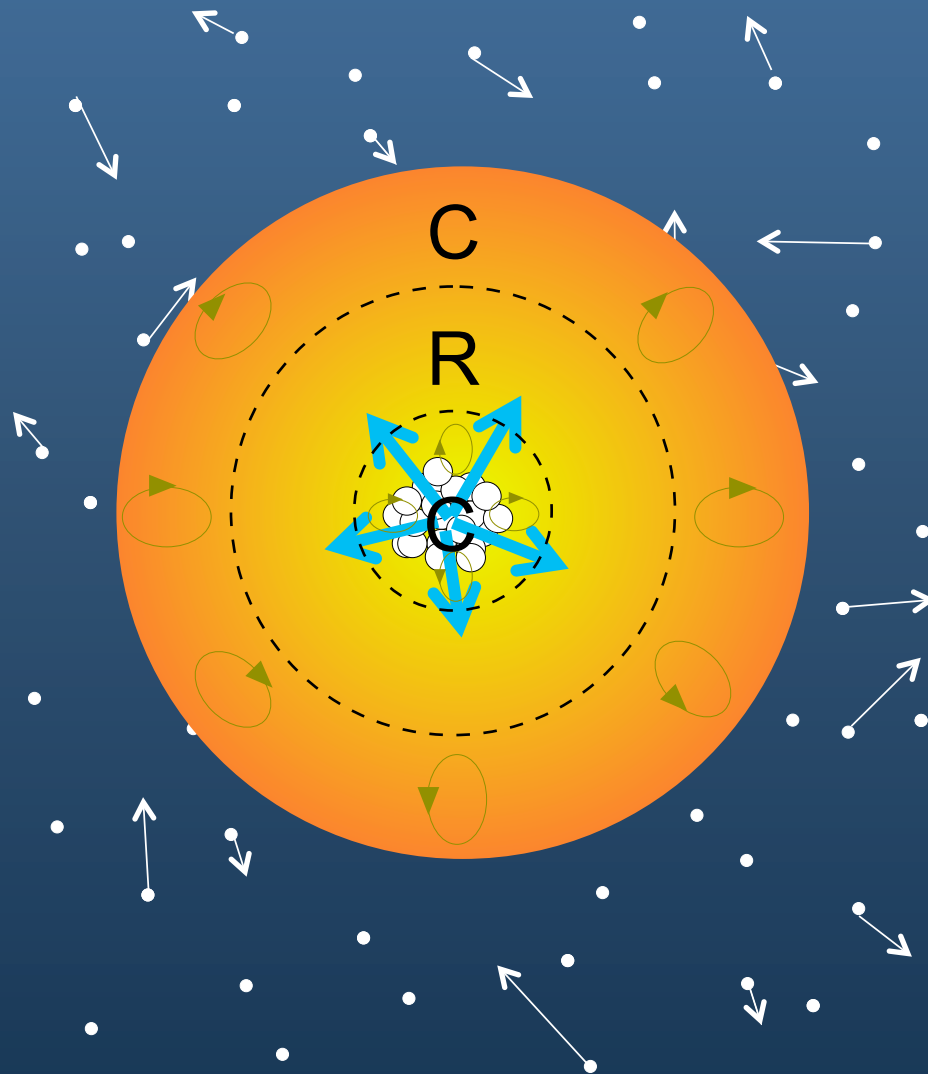
Impact of asymmetric Dark Matter on stars

Reduction central temperature

SUN: solar neutrinos, helioseismology

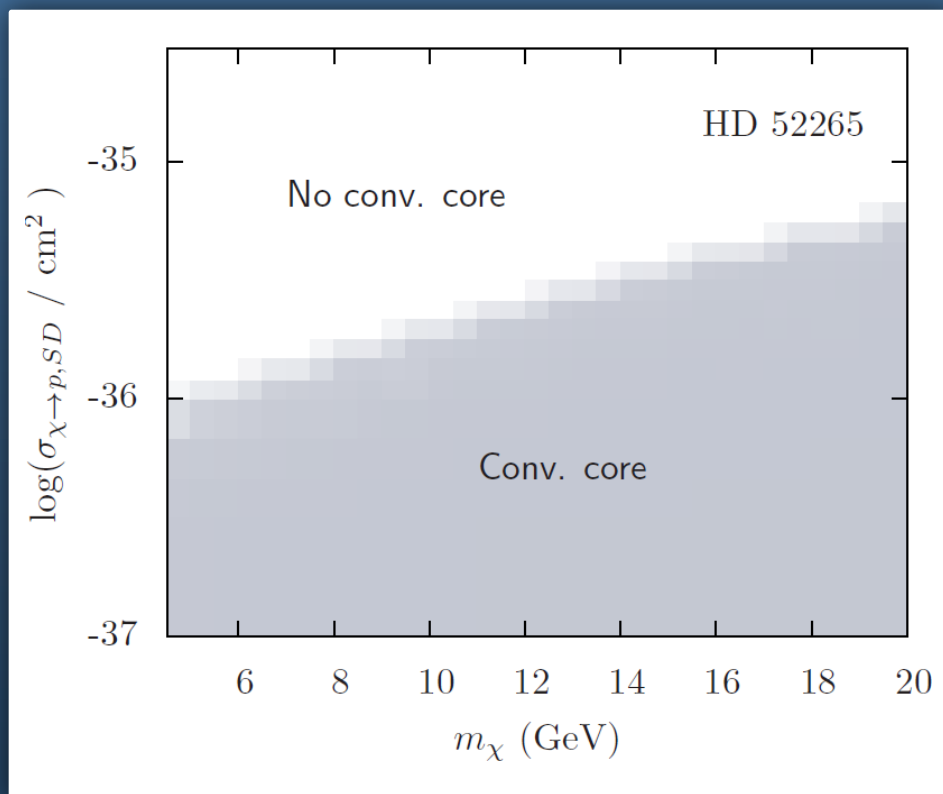
WHY OTHER STARS?

- $M_{\star} \downarrow \Rightarrow$ stronger DM impact
- Suppression of **convective core** in 1.1-1.3 $M_{\odot}$ stars



[Casanellas & Lopes , ApJL 765 (2013)]

Impact of asymmetric Dark Matter on stars

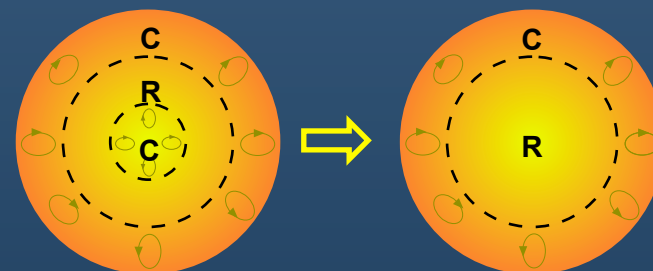


Reduction central temperature

SUN: solar neutrinos, helioseismology

WHY OTHER STARS?

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- Suppression of **convective core** in 1.1-1.3 $M_{\odot}$ stars



Convective Core in HD 52265 ??

[Ballot *et al.*, A&A 530 (2011), Escobar *et al.*, A&A 547 (2012)]

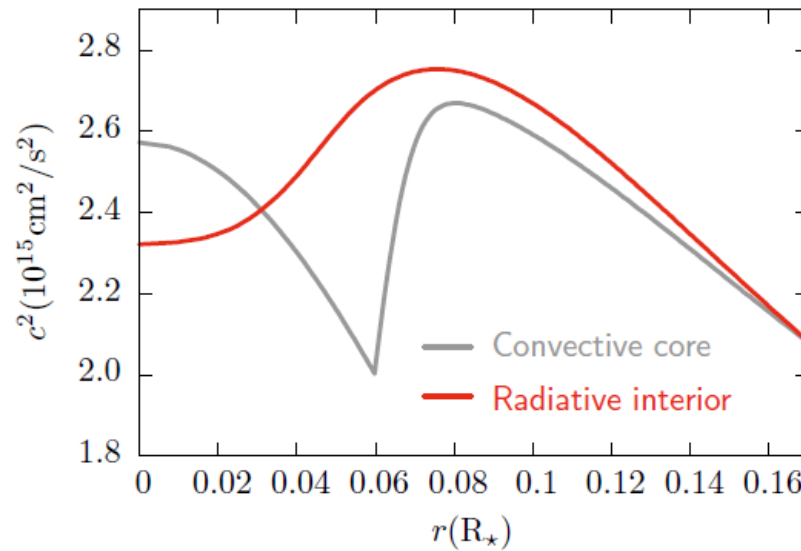
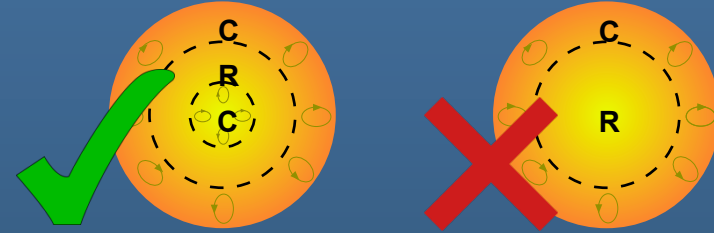
[Casanellas & Lopes, ApJL 765 (2013)]

Star	$M (M_{\odot})$	$R (R_{\odot})$	$L (L_{\odot})$	$T_{eff} (K)$	$(Z/X)_s$	$\langle \Delta \nu_{n,0} \rangle^a (\mu\text{Hz})$	$\langle \delta \nu_{02} \rangle^a (\mu\text{Hz})$
HD 52265							
Observ. [19, 23]	1.18-1.25 ^b	1.19-1.30 ^b	2.09 ± 0.24	6100 ± 60	0.028 ± 0.003	98.07 ± 0.19	8.18 ± 0.28
Stand. mod./DM mod. ^c	1.18	1.30	2.22	6170	0.028	97.92/98.05	8.16/7.65

Constraining asym Dark Matter with asteroseismology

- Presence or absence of a **convective core** in KIC 12009504 (Dushera)

[Silva Aguirre *et al.*, ApJL 769 (2013)]



$$dr_{0213} = 6 \left(\frac{D_{02}}{\Delta \nu_{n-1,1}} - \frac{D_{13}}{\Delta \nu_{n,0}} \right)$$

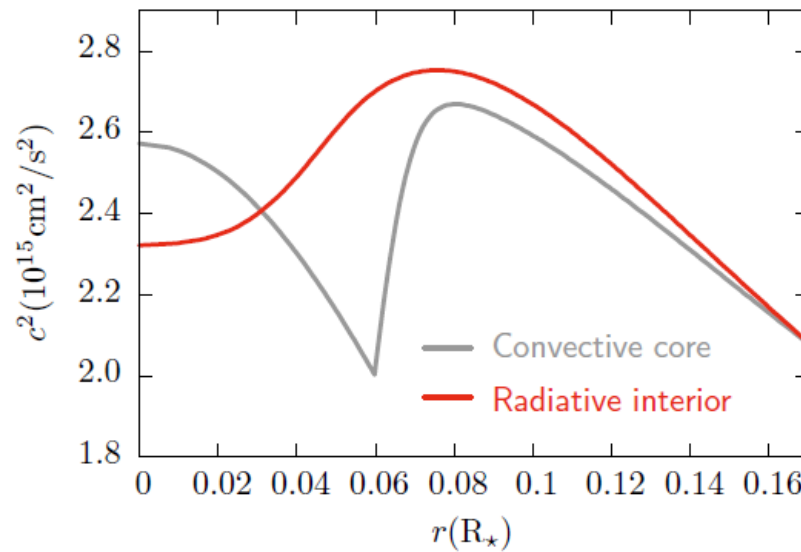
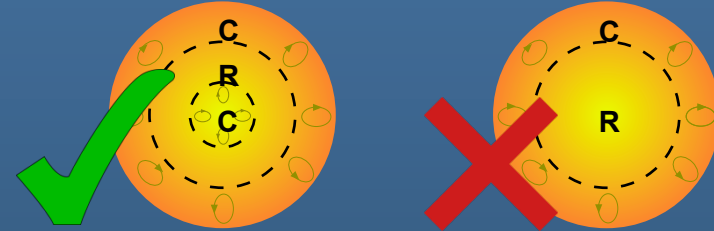
$$\text{where } D_{l,l+2} \equiv \delta \nu_{n,l} / (4l + 6)$$

[Cunha M.S. & Metcalfe T.S. (2007), Cunha M.S. & Brandão I.M (2014)]

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$$|S\{\Delta\nu\ r_{010}\}|$$

$$r_{01} = \frac{d_{01}}{\Delta\nu_{n,1}}, \quad r_{10} = \frac{d_{10}}{\Delta\nu_{n+1,0}},$$

where

$$d_{01} = \frac{1}{8}(\nu_{n-1,0} - 4\nu_{n-1,1} + 6\nu_{n,0} - 4\nu_{n,1} + \nu_{n+1,0}),$$

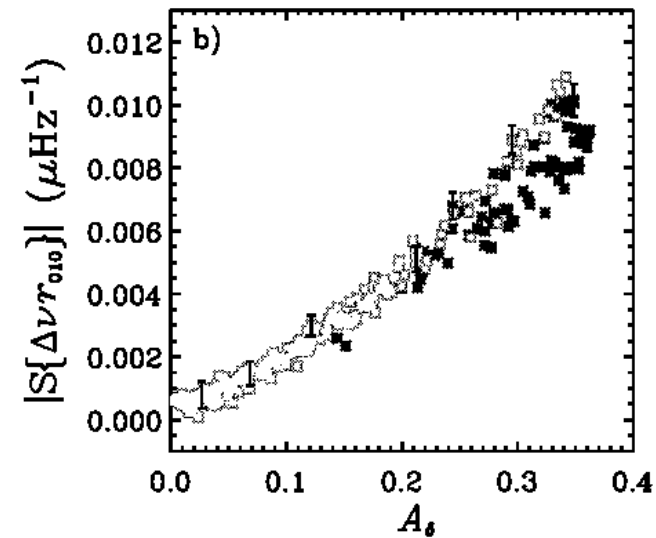
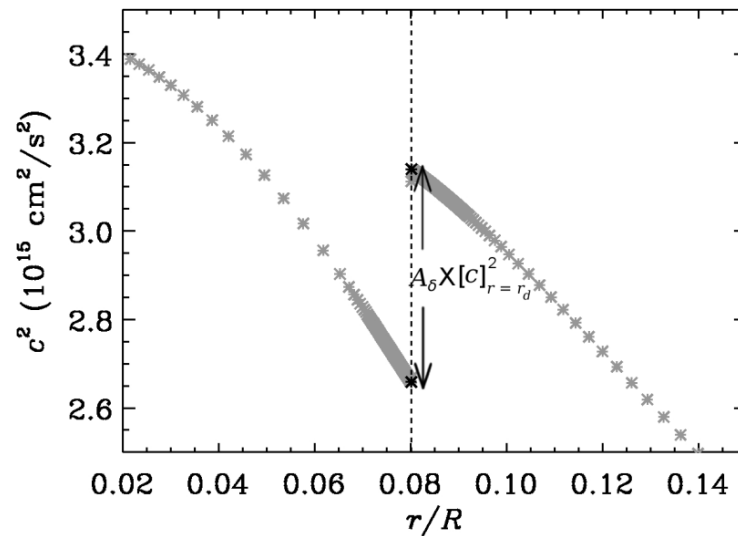
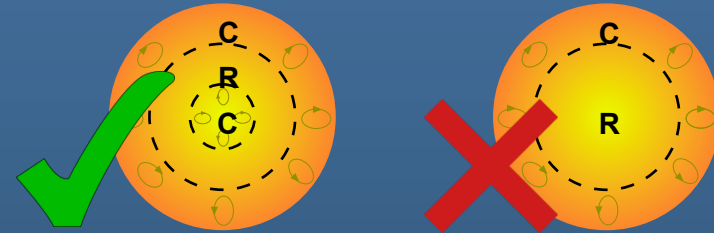
$$d_{10} = -\frac{1}{8}(\nu_{n-1,1} - 4\nu_{n,0} + 6\nu_{n,1} - 4\nu_{n+1,0} + \nu_{n+1,1}).$$

[Roxburgh I. W. & Vorontsov S. V. (2003), Brandao I., Cunha M. & Christensen-Dalsgaard J, MNRAS 438 (2014)]

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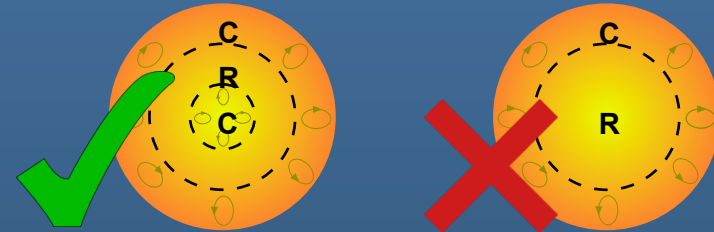
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[Silva Aguirre *et al.*, ApJL 769 (2013)]

- Modelling of Dushera: Grid with CESAM
[Casanellas & Brandao, in prep.] (M, Z, age, α_{CONV} , α_{OV})



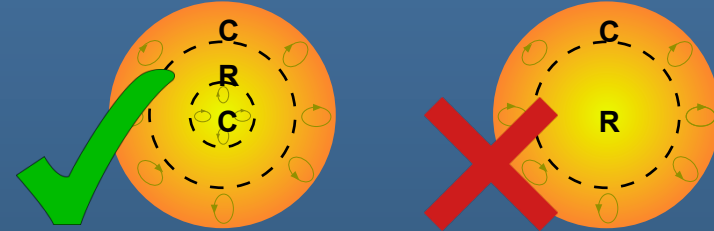
+

T_{eff}	$\log(g)$	Z/X_s^{-1}	$\langle \Delta\nu \rangle_{012}$
6200 ± 200	4.30 ± 0.2	0.023 ± 0.09	88 ± 0.6

Constraining asym Dark Matter with asteroseismology

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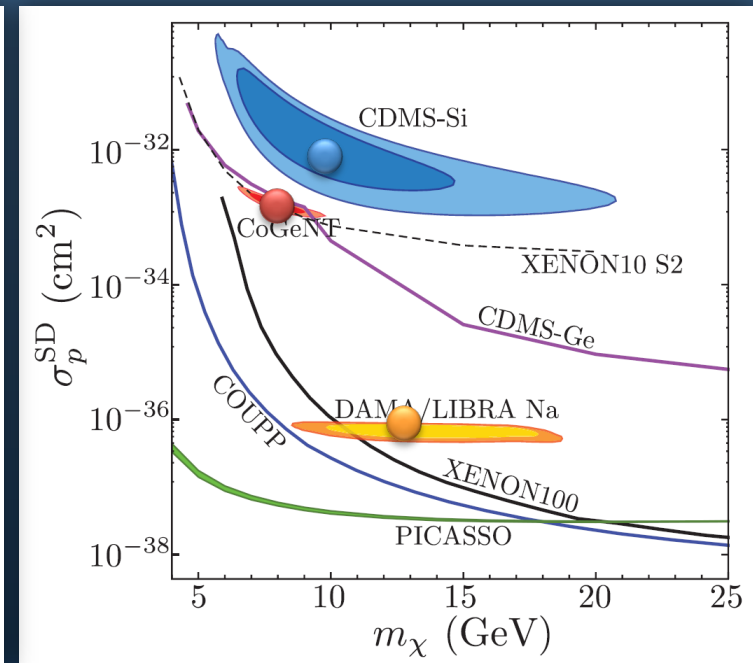
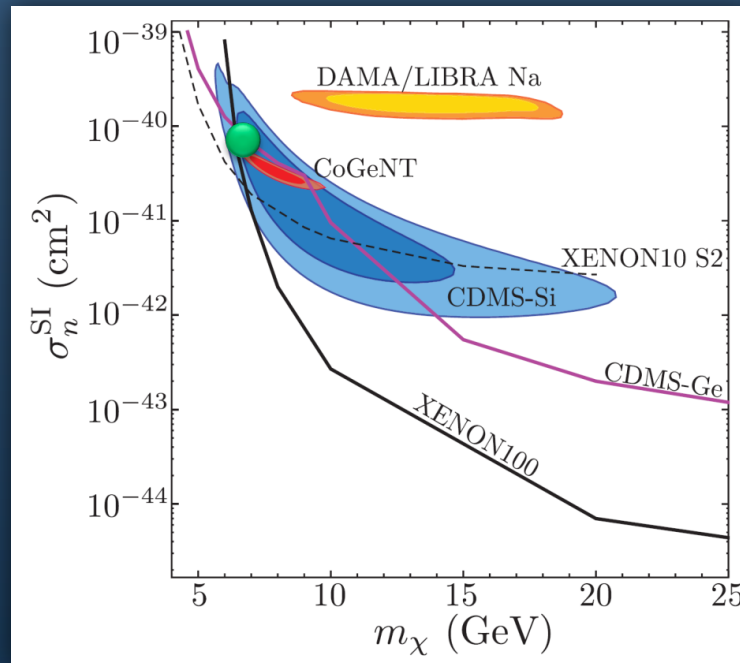
[Silva Aguirre *et al.*, ApJL 769 (2013)]



- Modelling of Dushera: Grid with CESAM (M, Z, age, α_{CONV} , α_{OV}) +

T_{eff}	$\log(g)$	Z/X_s	$\langle \Delta\nu \rangle_{012}$
6200 ± 200	4.30 ± 0.2	0.023 ± 0.09	88 ± 0.6

- DM model 1 (SI best fit)
- DM model 2 (DAMA)
- DM model 3 (CDMS)
- DM model 4 (CoGeNT)



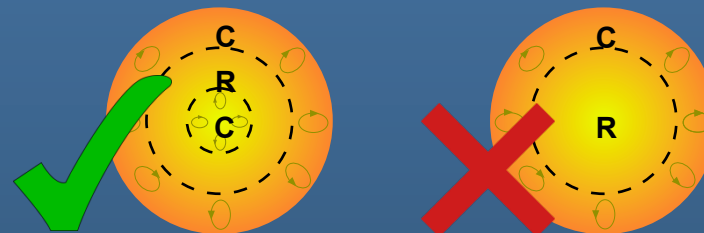
[Buckley M. & Lippincott W. H., Phys. Rev. D 88 (2013), Arina, arXiv:1310.5718, (2013)]

Jordi Casanellas, Toulouse 2014

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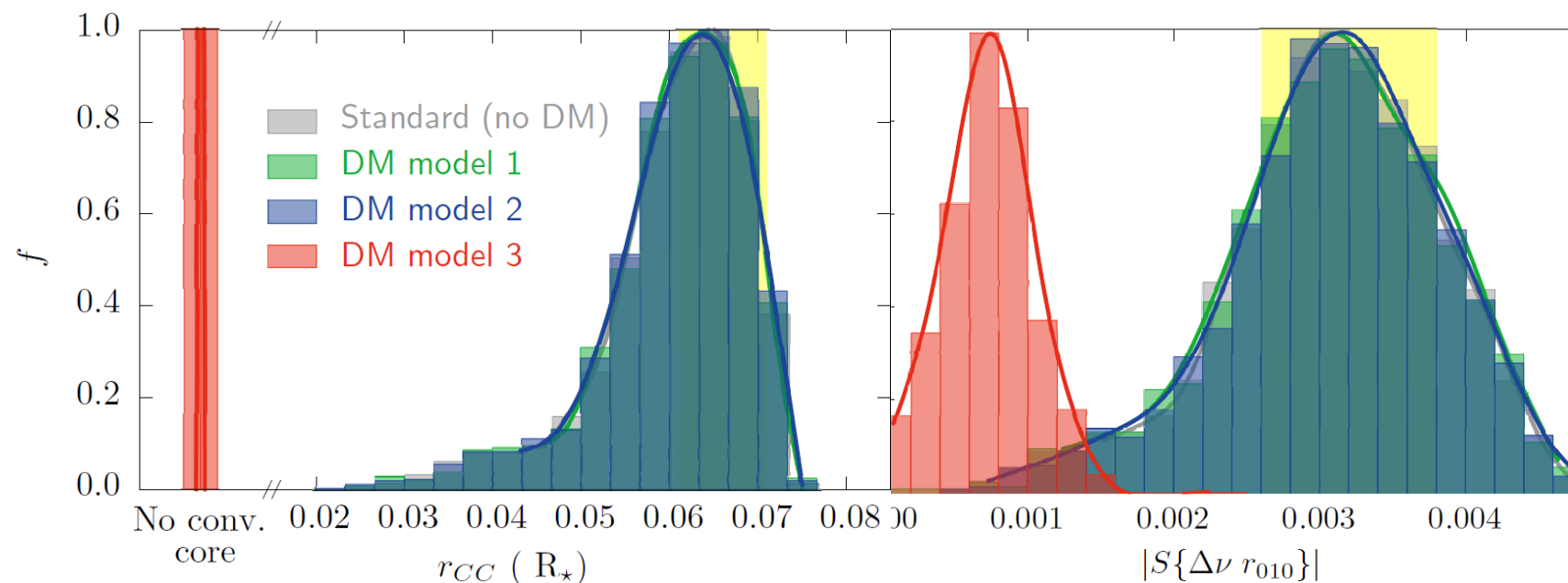
[Silva Aguirre *et al.*, ApJL 769 (2013)]



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+

T_{eff}	$\log(g)$	Z/X_s	$\langle \Delta\nu \rangle_{012}$
6200 ± 200	4.30 ± 0.2	0.023 ± 0.09	88 ± 0.6



WORK IN PROGRESS, see also POSTER #40

Conclusion:

ASTEROSEISMOLOGY can be used
to investigate **DARK MATTER**

Future directions:

- Solar-like oscillations in **low-mass stars** ($0.7 M_{\odot}$?) observed with high precision (detached eclipsing binaries?)
- Gravity modes in **Red Giants**
- Environments with **high Dark Matter densities**:
the Galactic Center, Globular Clusters, dwarf Sph Galaxies

Star	M ($M_{\odot}$)	R ($R_{\odot}$)	L ($L_{\odot}$)	T_{eff} (K)	$(Z/X)_s$	$\langle \Delta \nu_{n,0} \rangle^a$ (μHz)	$\langle \delta \nu_{02} \rangle^a$ (μHz)
KIC 8006161							
Observ. [19–21]	0.92-1.10 ^b	0.90-0.97 ^b	0.61 ± 0.02	5340 ± 70	0.043 ± 0.007	148.94 ± 0.13	10.10 ± 0.16
Stand. mod./DM mod. ^c	0.92	0.92	0.63	5379	0.039	149.03/149.08	10.12/9.13

Capture

Gould (1987)

$$C_{\chi}(t) = \int_0^{R_{\star}} 4\pi r^2 \int_0^{\infty} \frac{f(u)}{u} w \Omega_v^{-}(w) du dr$$

$$\Omega_v^{-}(w) = \sum_i \frac{\sigma_i n_i(r, t)}{w} \left(v_{esc, r}^2 - \frac{\mu_{-, i}^2}{\mu_i} u^2 \right) \theta \left(v_{esc, r}^2 - \frac{\mu_{-, i}^2}{\mu_i} u^2 \right)$$

$$\mu \equiv \frac{m_{\chi}}{m_n}, \quad \mu_{\pm} \equiv \frac{\mu \pm 1}{2} \quad \sigma_{\chi, i} = \sigma_{\chi, SI} A_i^2 \left(\frac{m_{\chi} m_{n, i}}{m_{\chi} + m_{n, i}} \right)^2 \left(\frac{m_{\chi} + m_p}{m_{\chi} m_p} \right)^2$$

$$\sigma_{\chi, H} = \sigma_{\chi, SI} + \sigma_{\chi, SD}.$$

$$\Omega_{v,i}^{-}(w) = \frac{\sigma_{\chi,i} n_i(r)}{w} \frac{2E_0}{m_{\chi}} \frac{\mu_{+,i}^2}{\mu_i} \left\{ \exp\left(-\frac{m_{\chi} u^2}{2E_0}\right) - \exp\left(-\frac{m_{\chi} u^2}{2E_0} \frac{\mu_i}{\mu_{+,i}^2}\right) \exp\left(-\frac{m_{\chi} v_e^2}{2E_0} \frac{\mu_i}{\mu_{-,i}^2} \left(1 - \frac{\mu_i}{\mu_{+,i}^2}\right)\right) \right\}$$

$$f_0(u) = \frac{\rho_{\chi}}{m_{\chi}} \frac{4}{\sqrt{\pi}} \left(\frac{3}{2}\right)^{3/2} \frac{u^2}{\bar{v}_{\chi}^3} \exp\left(-\frac{3u^2}{2\bar{v}_{\chi}^2}\right)$$

$$f_{v_{\star}}(u) = f_0(u) \exp\left(-\frac{3v_{\star}^2}{2\bar{v}_{\chi}^2}\right) \frac{\sinh(3uv_{\star}/\bar{v}_{\chi}^2)}{3uv_{\star}/\bar{v}_{\chi}^2}$$

Equilibrium between capture and annihilation rates

$$\frac{dN_\chi}{dt} = C_\chi - 2A_\chi N_\chi^2 - E_\chi N_\chi \quad A_\chi = 4\pi \int_0^{R_\star} r^2 \frac{\langle \sigma_a v \rangle n_\chi^2}{2} dr$$

$$N_\chi(t) = C_\chi \tau_{\chi,eq} \tanh\left(\frac{t}{\tau_{\chi,eq}}\right) \quad \text{Equilibrium timescale: } \tau_{\chi,eq} \approx \sqrt{\pi^{3/2} r_\chi^3 / (C_\chi \langle \sigma_a v \rangle)}$$

WIMPs distribution inside the star:

$$n_\chi(r) = \pi^{-3/2} r_\chi^{-3} e^{-r^2/r_\chi^2} \quad r_\chi = \sqrt{3\kappa_B T_c / 2\pi G \rho_c m_\chi}$$

$$n_\chi(r) = \frac{T(r)^{3/2}}{T_c} \exp\left(-\int \frac{k_B \alpha(r) \frac{dT}{dr} + m_\chi \frac{d\phi}{dr}}{k_B T(r)} dr\right)$$

Rate of energy production by DM annihilation:

$$\varepsilon_\chi(r) = f_\chi (2m_\chi) \rho(r)^{-1} \frac{\langle \sigma_a v \rangle n_\chi(r)^2}{2} \quad L_{\chi,prod} = \frac{2}{3} C_\chi m_\chi$$

Energy transport (DM cooling):

$$L_{\chi,trans}(r) = 4\pi r^2 n_\chi(r) l_\chi \kappa(r) \left(\frac{k_B T(r)}{m_\chi}\right)^{1/2} k_B \frac{dT}{dr} f(K) h(r)$$

Frequencies of the acoustic modes:

$$\nu_{n,l} \simeq \left(n + \frac{l}{2} + \epsilon_v\right) \nu_0 + O(\nu^{-2}), \quad \nu_0 = [2 \int_0^R dr/c]^{-1}$$

Large separation: $\Delta \nu_{n,l} = \nu_{n,l} - \nu_{n-1,l} \simeq \nu_0$.

Small separation: $\delta \nu_{n,l} = \nu_{n,l} - \nu_{n-1,l+2}$,

Combinations to detect the convective core:

$$r_{01} = \frac{d_{01}}{\Delta \nu_{n,1}}, \quad r_{10} = \frac{d_{10}}{\Delta \nu_{n+1,0}}, \quad \text{Roxburgh \& Vorontsov (2003)}$$

where Silva Aguirre et. al (2010)

$$d_{01} = \frac{1}{8}(\nu_{n-1,0} - 4\nu_{n-1,1} + 6\nu_{n,0} - 4\nu_{n,1} + \nu_{n+1,0}),$$

$$d_{10} = -\frac{1}{8}(\nu_{n-1,1} - 4\nu_{n,0} + 6\nu_{n,1} - 4\nu_{n+1,0} + \nu_{n+1,1}).$$

$$dr_{0213} \equiv \frac{D_{02}}{\Delta \nu_{n-1,1}} - \frac{D_{13}}{\Delta \nu_{n,0}},$$

where $D_{l,l+2} \equiv \delta \nu_{n,l}/(4l+6)$ Cunha & Metcalfe (2007)

Hidro. Eq.: $\frac{dP}{dr} = -\rho(r) \frac{GM(r)}{r^2}$

Therm. Eq.: $\frac{dL}{dr} = 4\pi r^2 \rho(r) \varepsilon(r)$ (rates and cross sections for pp, CNO and 3-alpha reactions)

Energy transport: $\frac{dT}{dr} = -\frac{L(r)}{4\pi r^2} \frac{\kappa_{cm}}{T^3} \frac{3}{16\sigma}$ (radiative)
when $\nabla_{ad} < \nabla_{rad}$

$\frac{dT}{dr} = \nabla_{ad} \frac{T}{P} \frac{dP}{dr}$ (convective)
when $\nabla_{ad} > \nabla_{rad}$

Continuity: $\frac{dm}{dr} = 4\pi r^2 \rho(r)$

Boundary: $T(r=R) = 0$ $M(r=0) = 0$
 $P(r=R) = 0$ $L(r=0) = 0$

Equation of state: Tabulated (mixture, X,Y, p, ρ , T)

Opacities: Tabulated

Solar composition

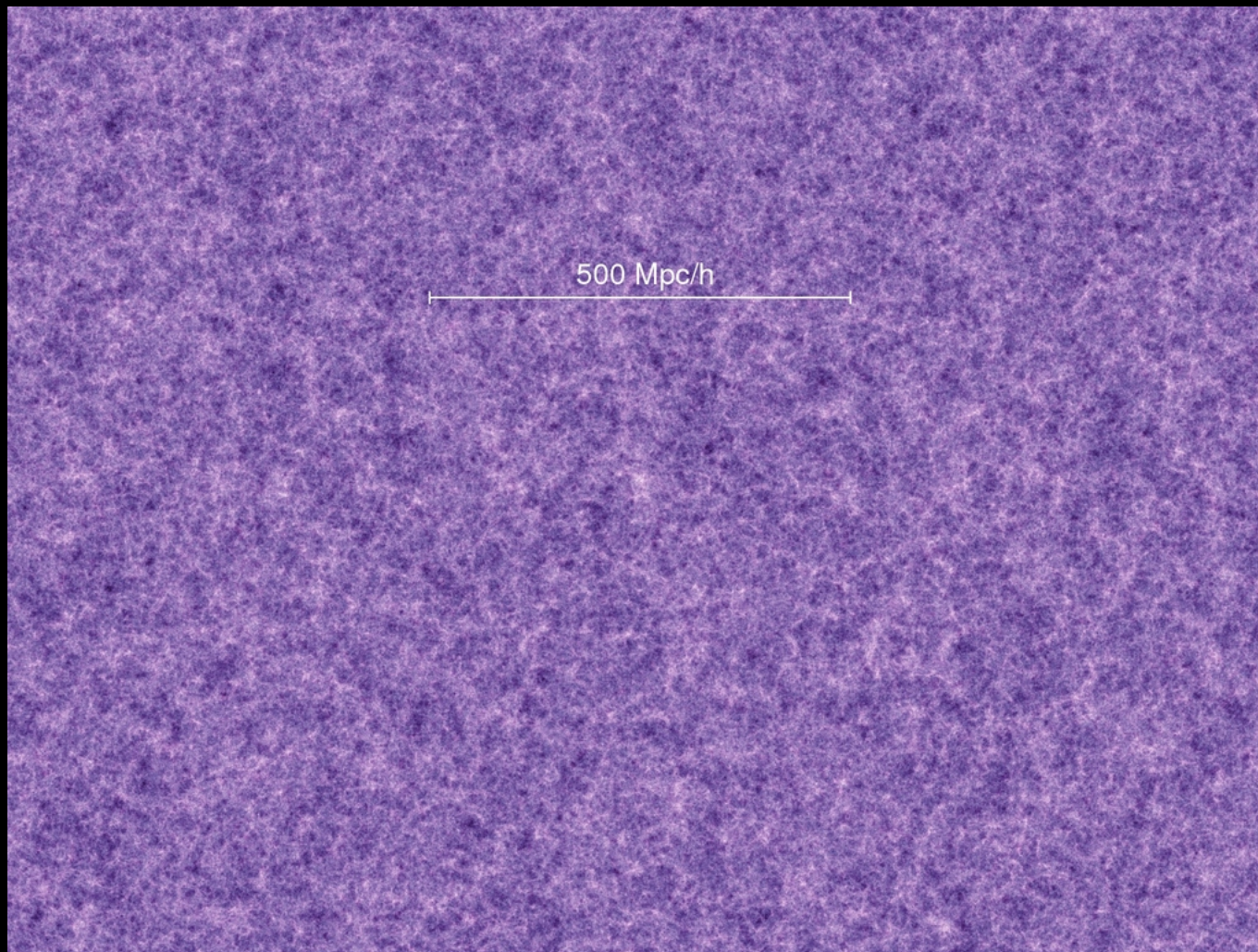
Chemical evolution

TABLE I. Variations in the total capture rate, C_χ , and in the ratio between the luminosities from DM annihilations and thermonuclear reactions, L_χ/L_{nuc} , when there is an uncertainty of 10% in the knowledge of one parameter of the DM characteristics or of the stellar structure. If not stated otherwise, we assumed a halo of DM particles with a mass $m_\chi = 100$ GeV, a velocity dispersion $\bar{v}_\chi = 270$ km s $^{-1}$, and a star of $1M_\odot$ in the middle of the MS, with a metallicity $Z = 0.019$ and a velocity $v_\star = 220$ km s $^{-1}$.

	C_χ		L_χ/L_{nuc}	
$m_\chi = 5$ GeV $\pm 10\%$	-10%	+12%	-1%	+1%
$m_\chi = 500$ GeV $\pm 10\%$	-18%	+23%	-9%	+11%
$\bar{v}_\chi = 100$ km s $^{-1}$ $\pm 10\%$	+6%	-7%	+6%	-7%
$\bar{v}_\chi = 500$ km s $^{-1}$ $\pm 10\%$	-20%	+26%	-20%	+26%
$v_\star = 100$ km s $^{-1}$ $\pm 10\%$	-3%	+3%	-3%	+3%
$v_\star = 500$ km s $^{-1}$ $\pm 10\%$	-58%	+120%	-58%	+120%
$M_\star = 0.5M_\odot$ $\pm 10\%$	+26%	-22%	-20%	+26%
$M_\star = 7M_\odot$ $\pm 10\%$	+16%	-13%	-16%	+26%
$Z = 0.0004 \pm 10\%$	-0.1%	+0.1%	+2%	-0.3%
$Z = 0.04 \pm 10\%$	-2%	+2%	-2%	+1%

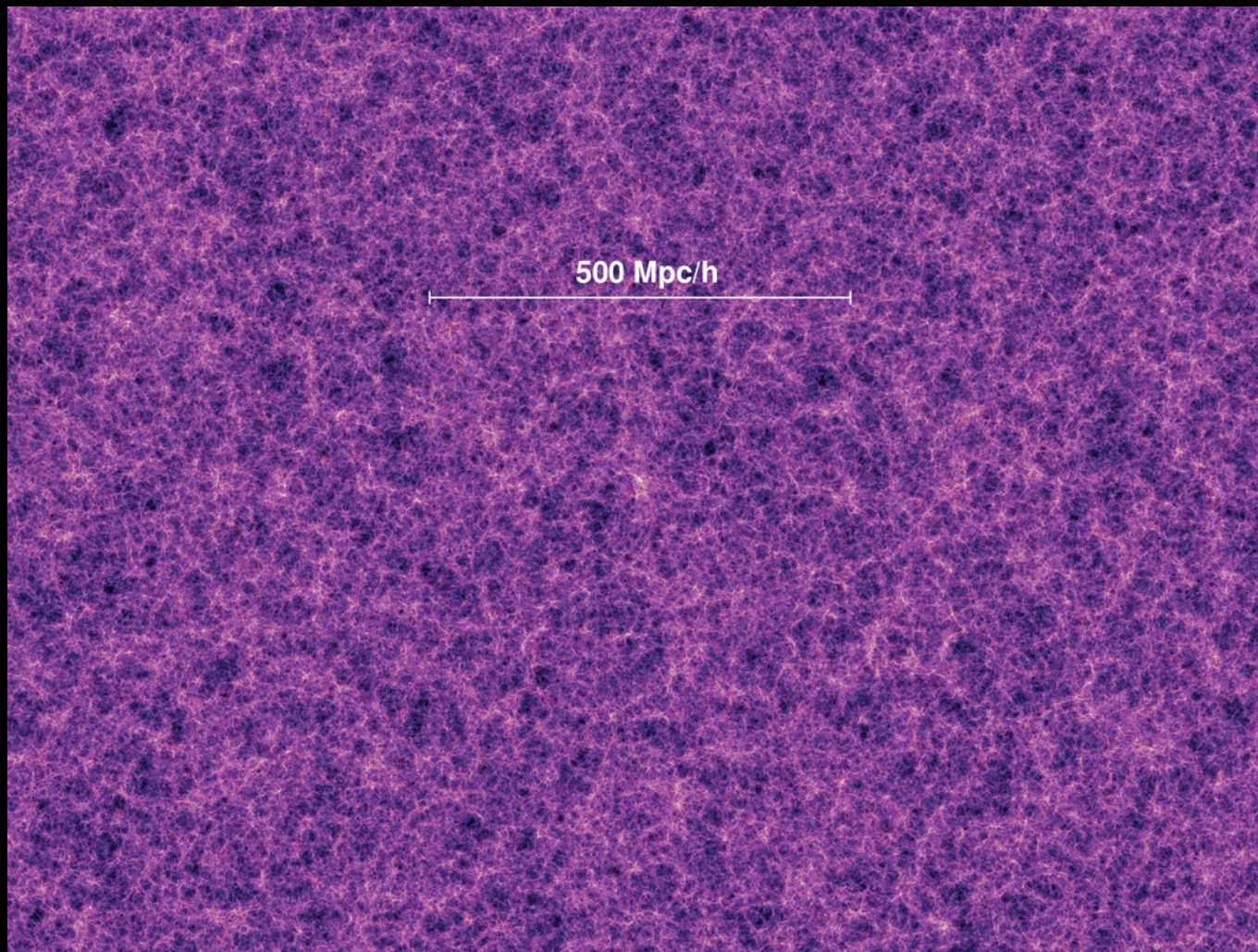
TABLE II. Variations in the capture rate due to SD and SI interactions of the stellar elements with the DM particles ($C_{\chi,\text{SI}}$ and $C_{\chi,\text{SD}}$) when there is an uncertainty of 10% in the knowledge of the mass of the DM particles or on the stellar metallicity.

	$C_{\chi,\text{SD}}$		$C_{\chi,\text{SI}}$	
$m_\chi = 100$ GeV $\pm 10\%$	-16%	+22%	-10%	+13%
$Z = 0.019 \pm 10\%$	-2%	+2%	+8%	-8%



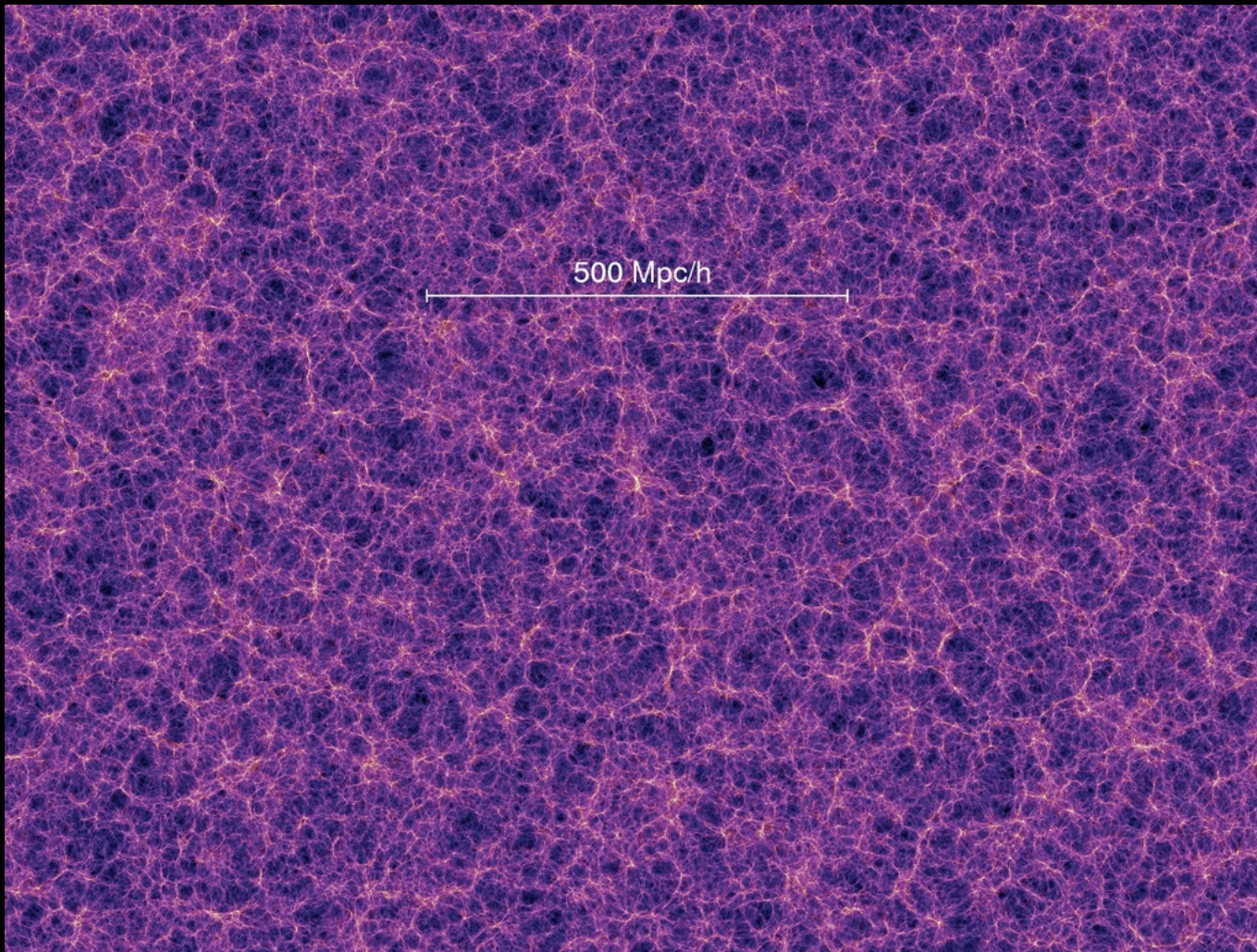
Redshift $z=18.3$ ($t = 0.21$ Gyr)

Millenium Simulation [Springel *et al.*, Nature 435 (2005)]



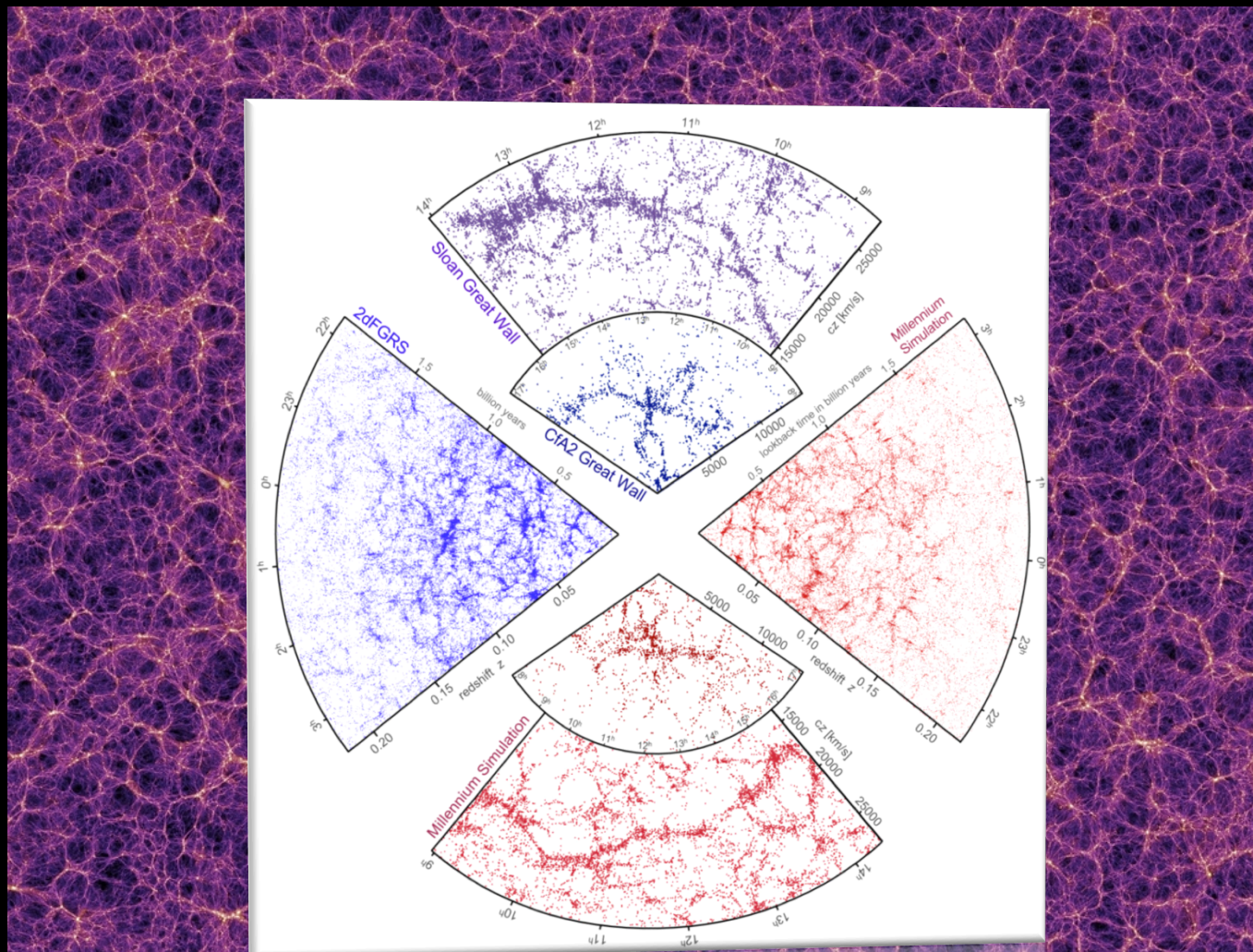
Redshift $z=5.7$ ($t = 1.0$ Gyr)

Millenium Simulation [Springel *et al.*, Nature 435 (2005)]



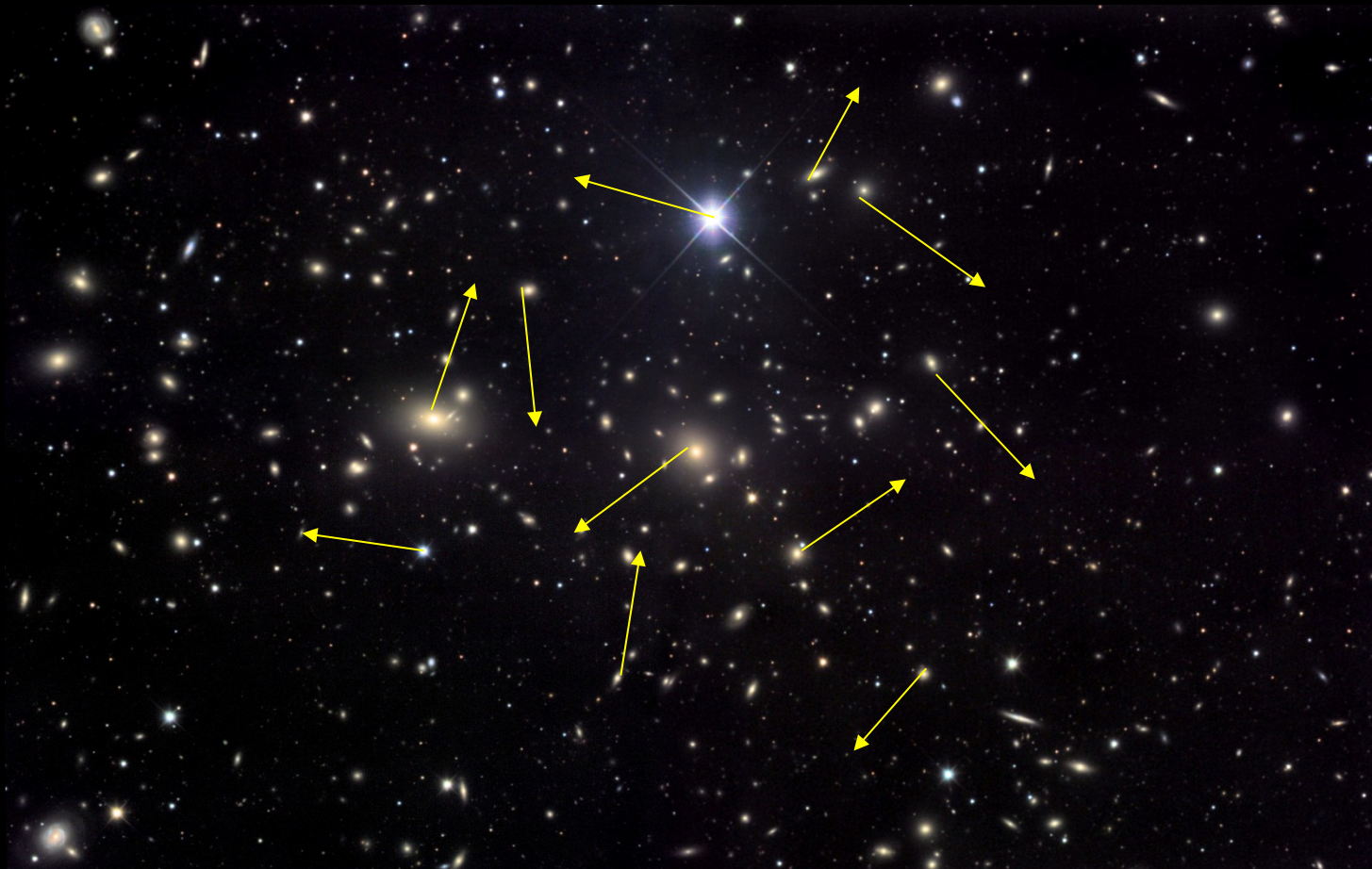
Redshift $z=1.4$ ($t = 4.7$ Gyr)

Millenium Simulation [Springel *et al.*, Nature 435 (2005)]



Redshift $z=0$ ($t = 13.6$ Gyr)

Millenium Simulation [Springel, et al., Nat, 425 (2003), 40 (2006)]

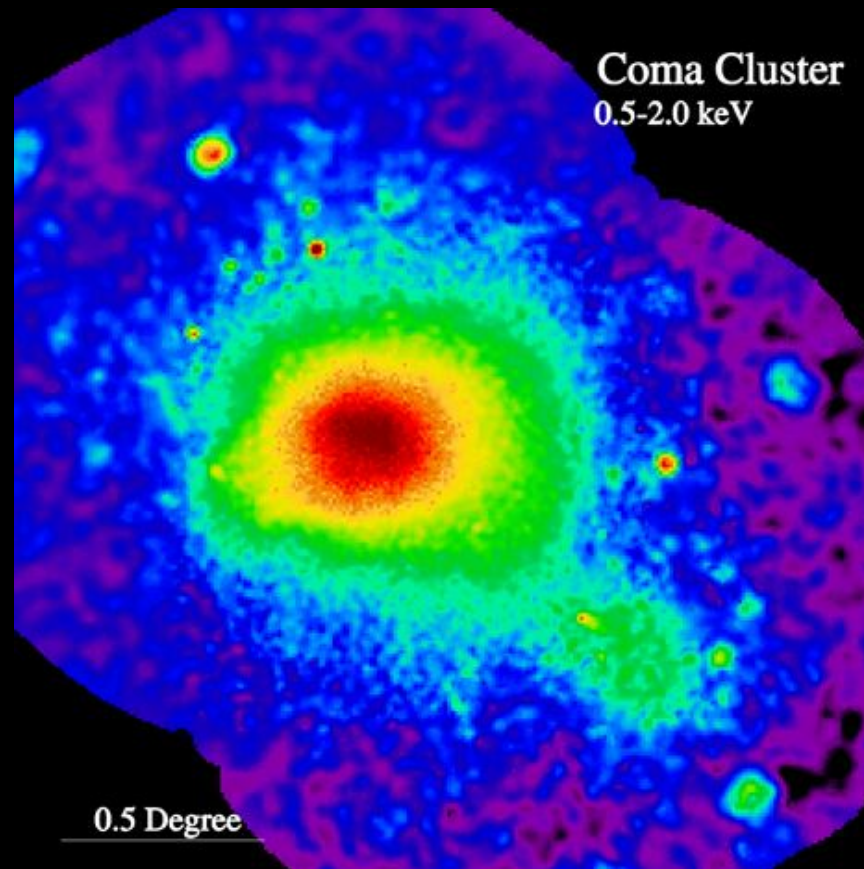


Dark Matter = 400 x Luminous Matter

[Zwicky, Helvetica Physica Acta 6 (1933)]

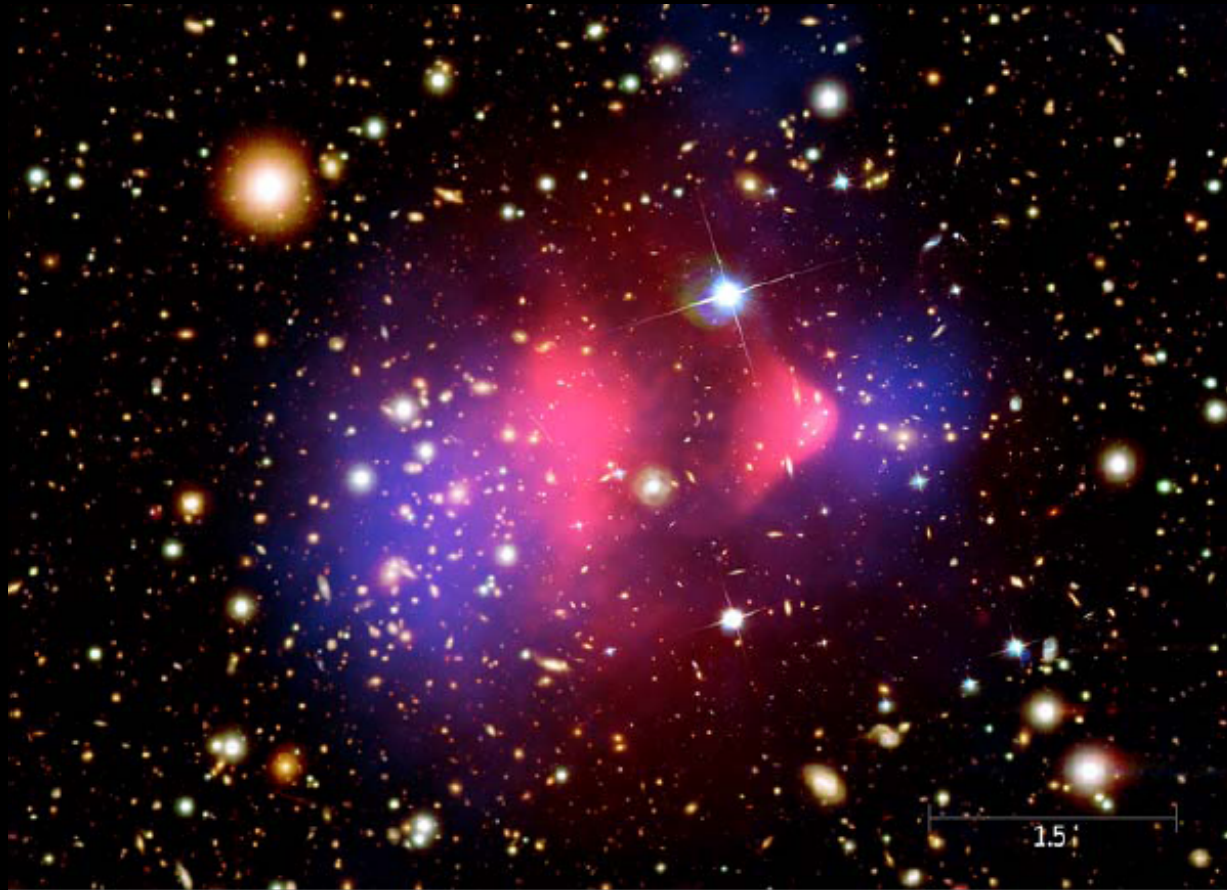
Coma Cluster

[Jim Misti, Misti Mountain Observatory]



X-rays from ROSAT telescope

[Voges *et al.*, *Astron.Astrophys.* 349 (1999)]



[Clowe *et al.*, ApJ 648 (2006), Mészáros *et al.*, MNRAS 365 (2006), Clowe *et al.*, ApJ 648 (2006)]