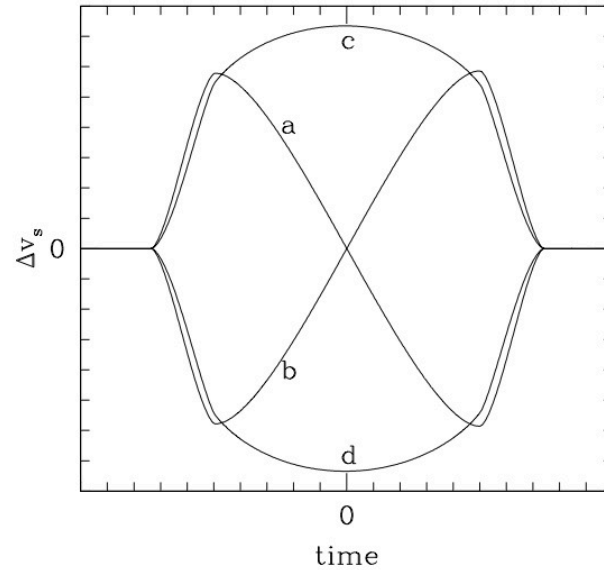
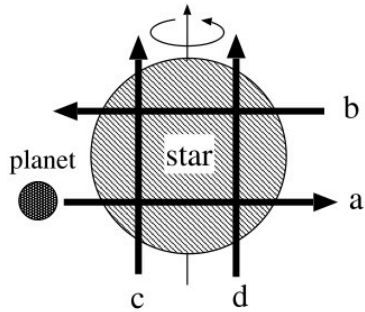


*Three dimensional spin-orbit determination:
joint analysis by asteroseismology, transit
lightcurve and Rossiter-McLaughlin effect*

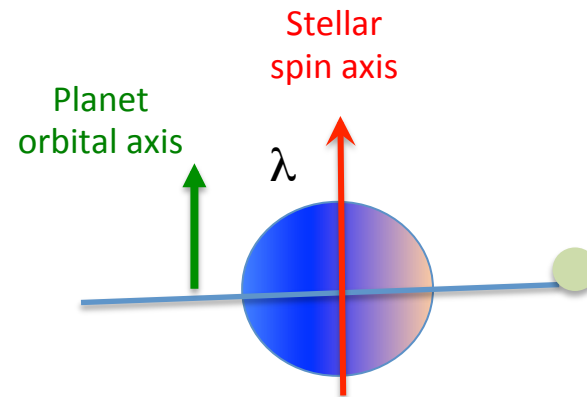
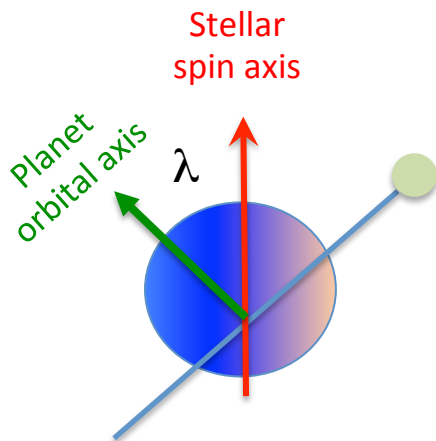
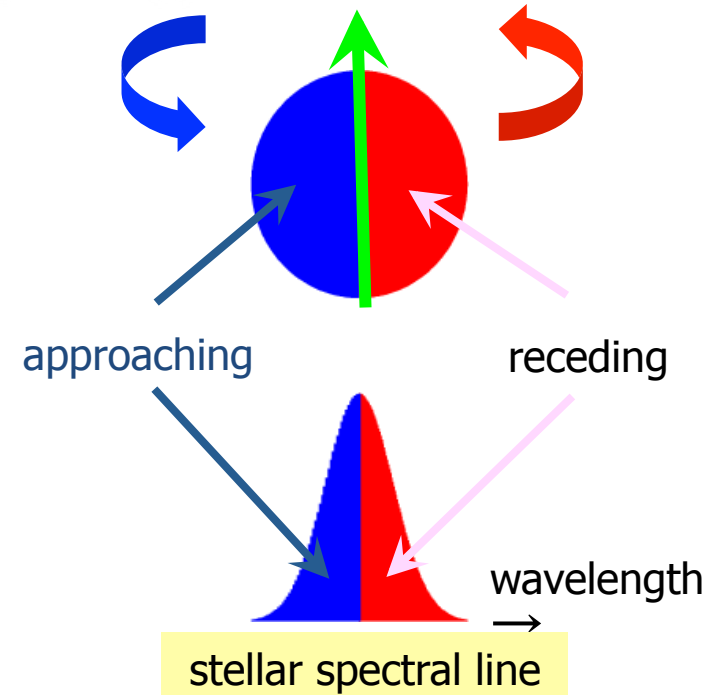
Benomar et al. (2014), accepted in PASJ

In collaboration with: Kento Masuda, Hiromoto Shibahashi, Yasushi Suto

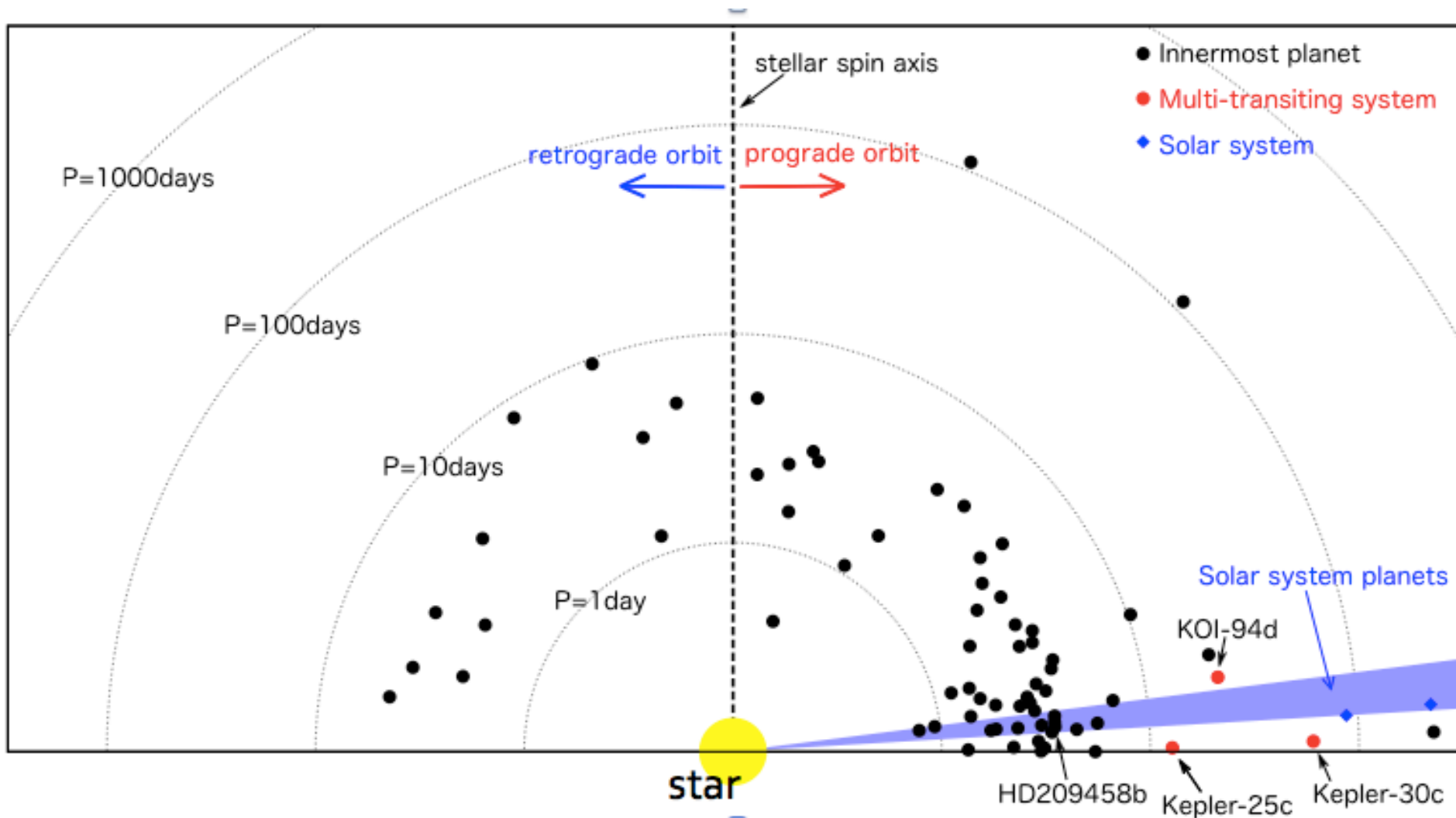
Rossiter McLaughlin effect



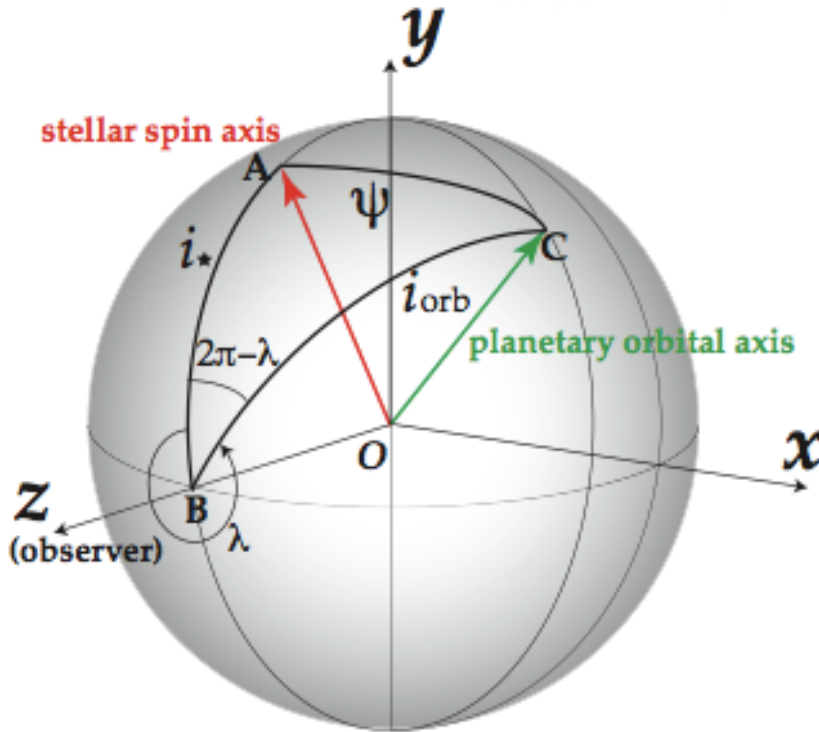
Ohta, Taruya & Suto, 2005



Proxy of misalignment using RM effect (λ)



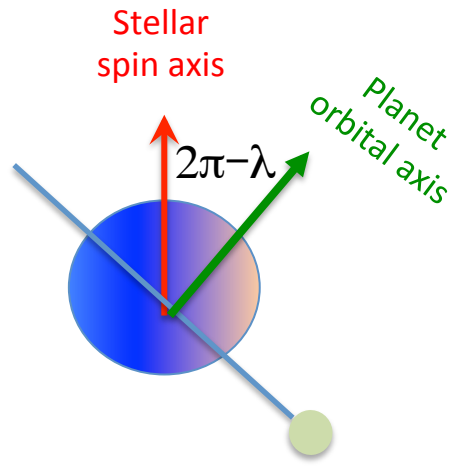
3D spin-orbit angle



- Ψ : Planet orbital plan relative to the stellar spin axis
- λ : Projection of Ψ into the sky plane
- i_{orb} : angle between the orbital plan and the observer
- i_* : angle between observer and stellar spin axis

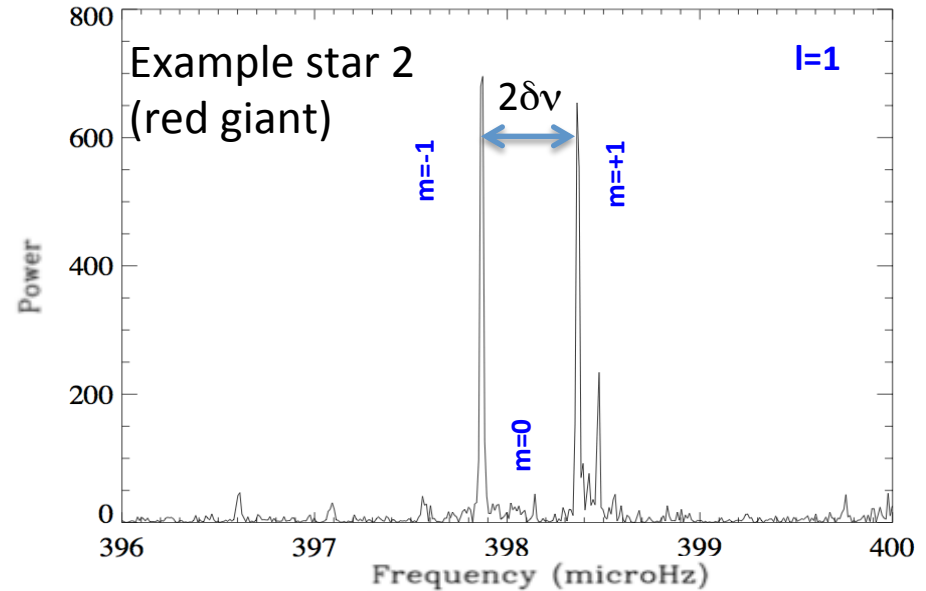
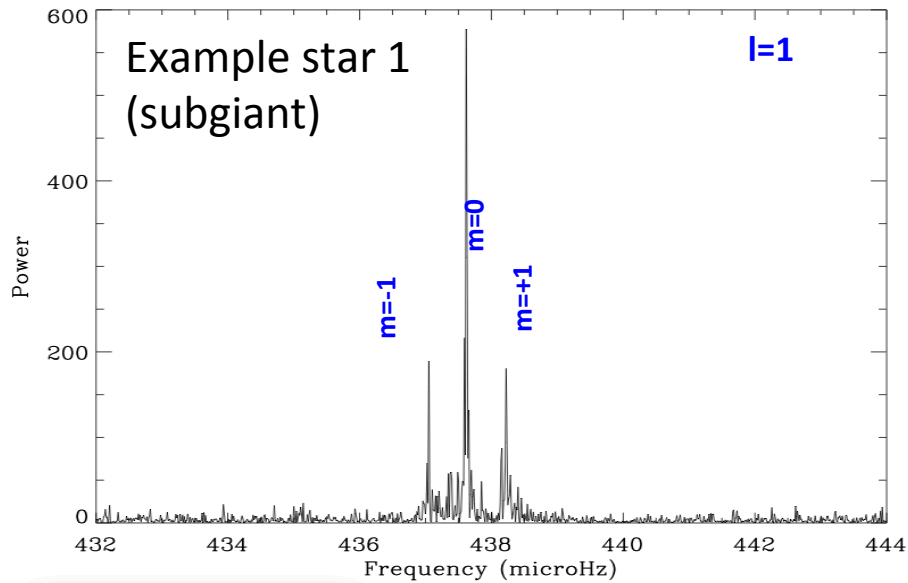
Observations give us:

- λ : Rossiter Mclaughin effect
- i_{orb} : The transit imposes $i_{\text{orb}} \sim 90$ degree
- i_* : Asteroseismology

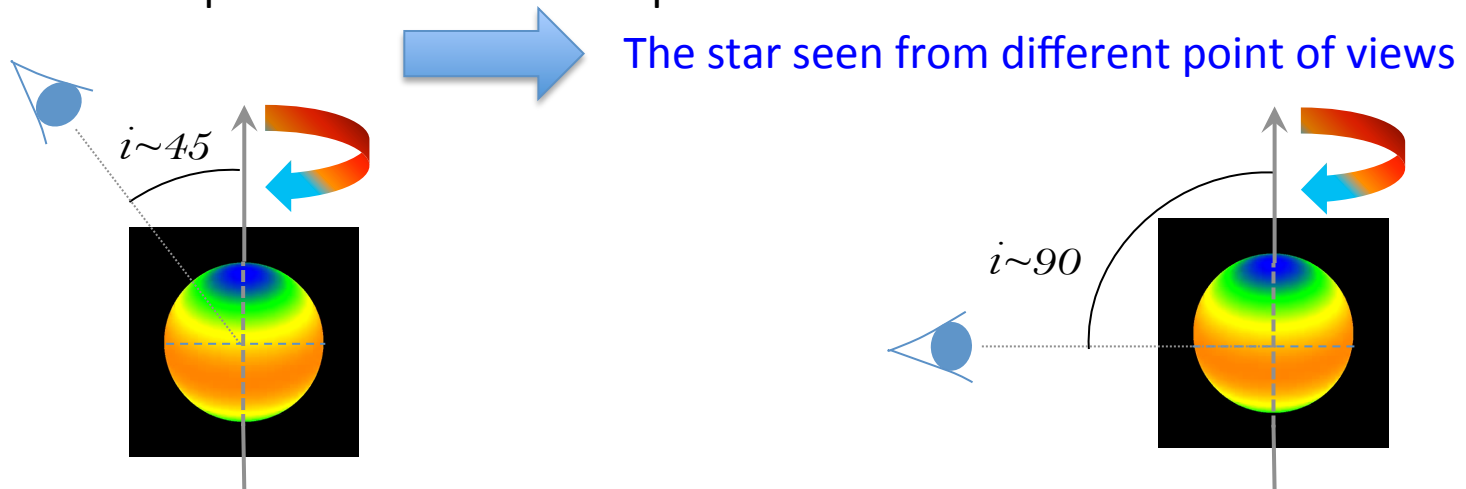


Measure of the stellar inclination

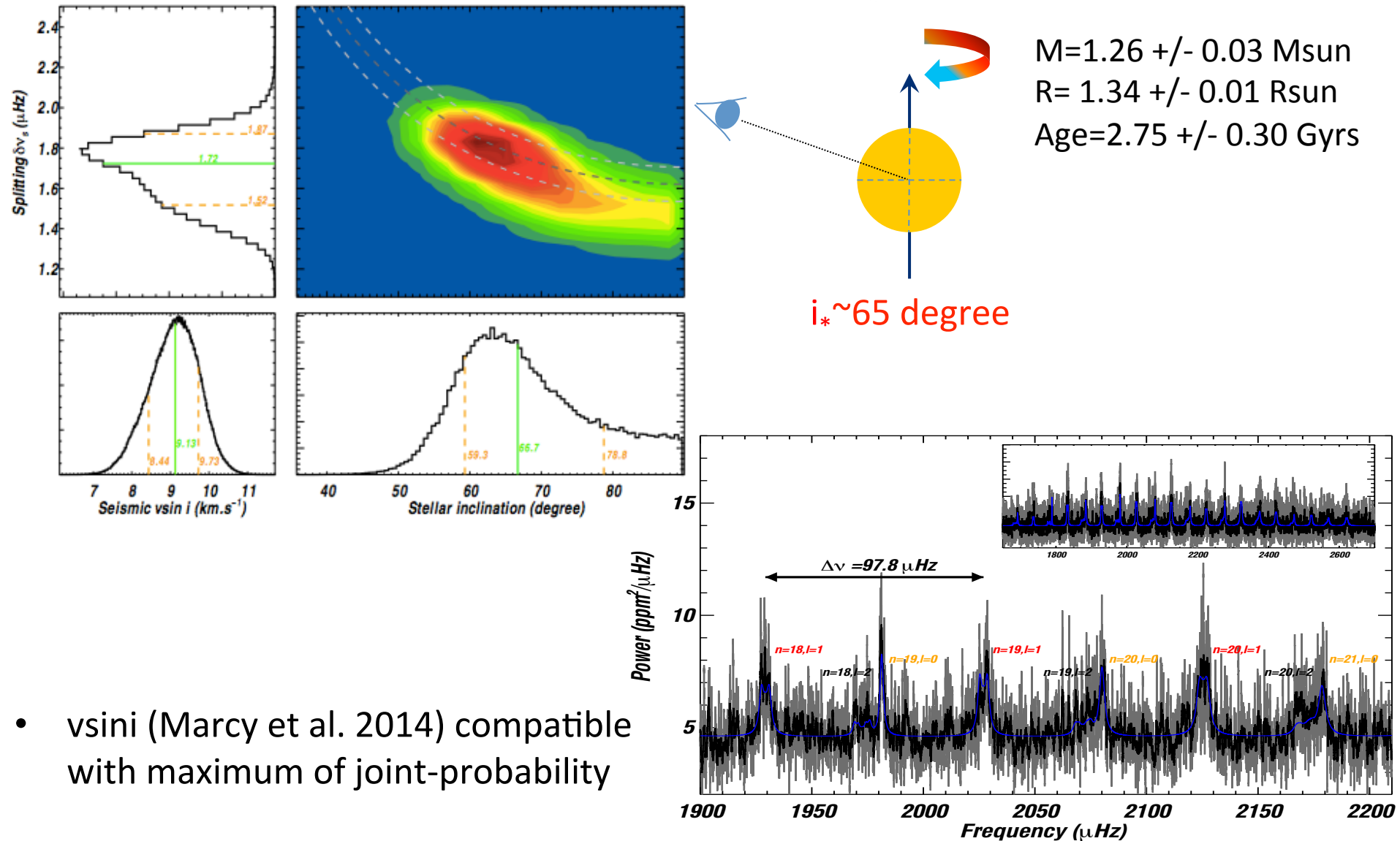
$$\nu_{n,l,m} = \nu_{n,l,0} + m\delta\nu_{n,l}$$



Why different amplitudes for the m -components of these $l=1$?



Kepler 25: Two neptunes in transit + one non-transiting planet



- $v \sin i$ (Marcy et al. 2014) compatible with maximum of joint-probability

Kepler 25: Two neptunes in transit + one non-transiting planet

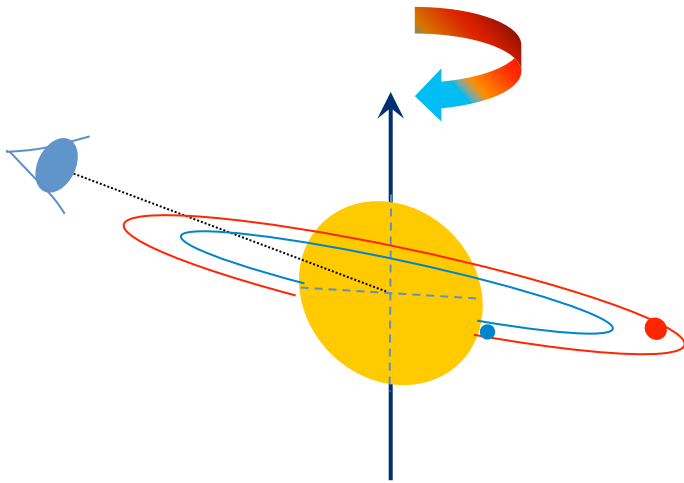
$$i_* = 65.4^{+10.6} \text{ degree}$$

$$\cos i_{\text{orb}} \sim 0.04788(38)$$

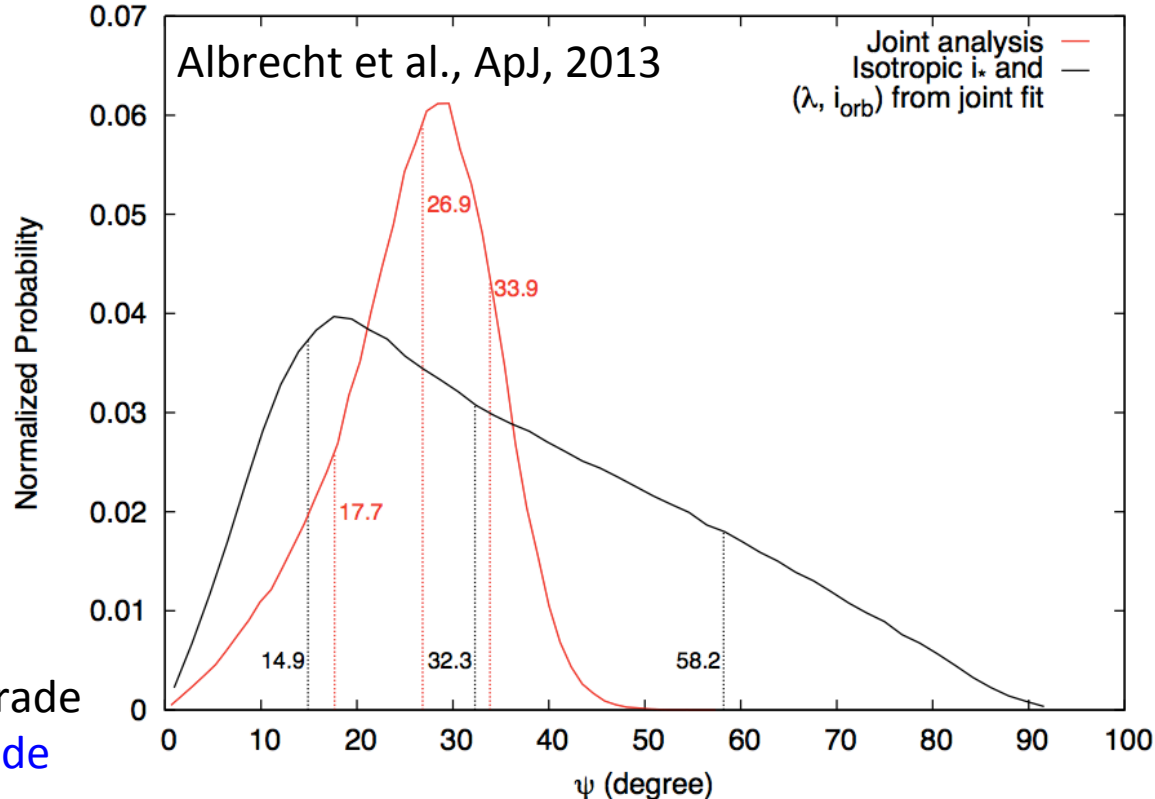
$\lambda \sim 9.4 \pm 7.1$ (reanalysis of RM from Albrecht et al. 2013) \rightarrow suggests a flat system

$\psi \sim 26.9^{+7.0}_{-9.2}$ degree \rightarrow Not so flat!

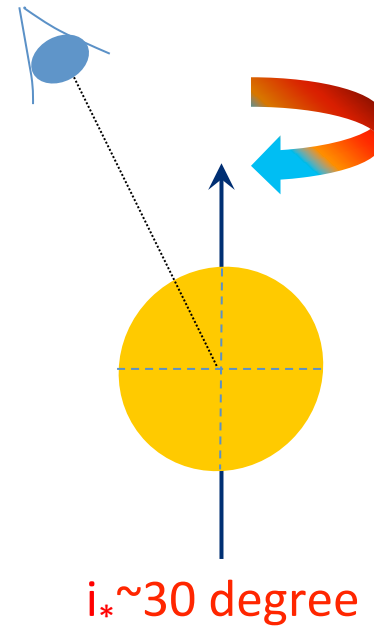
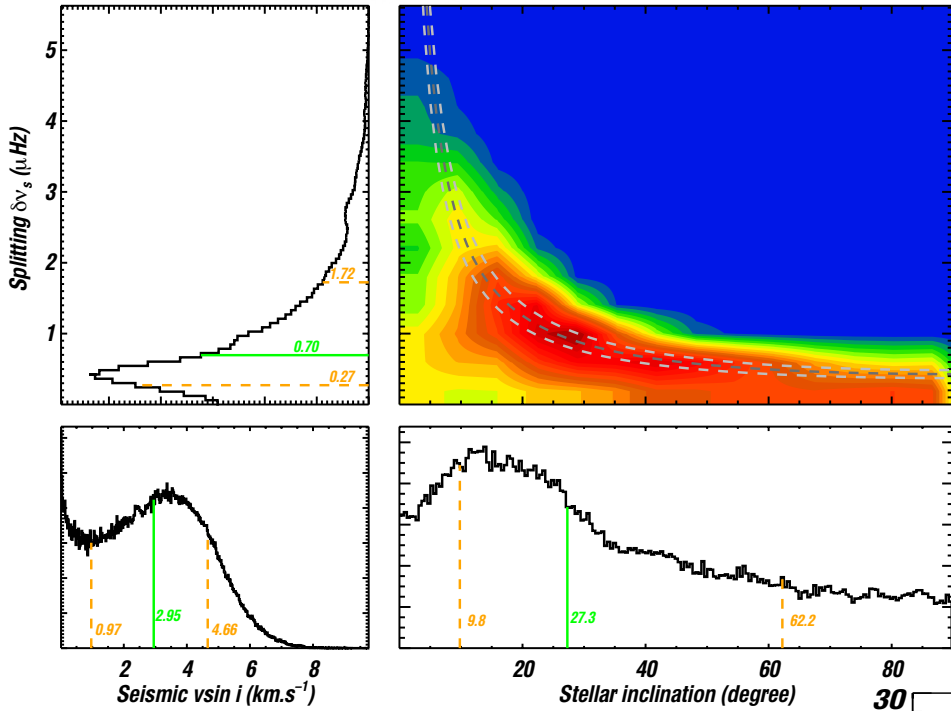
$$\psi_{\text{sun}} \sim 7 \text{ degree}$$



- \rightarrow If $|\Psi| > 90$ then the orbit is retrograde
- \rightarrow If $|\Psi| < 90$ then the orbit is prograde



HAT-P-7: a system with a hot Jupiter



$M = 1.59 \pm 0.03 M_{\text{sun}}$
 $R = 2.02 \pm 0.02 R_{\text{sun}}$
 Age = 1.7 ± 0.1 Gyrs

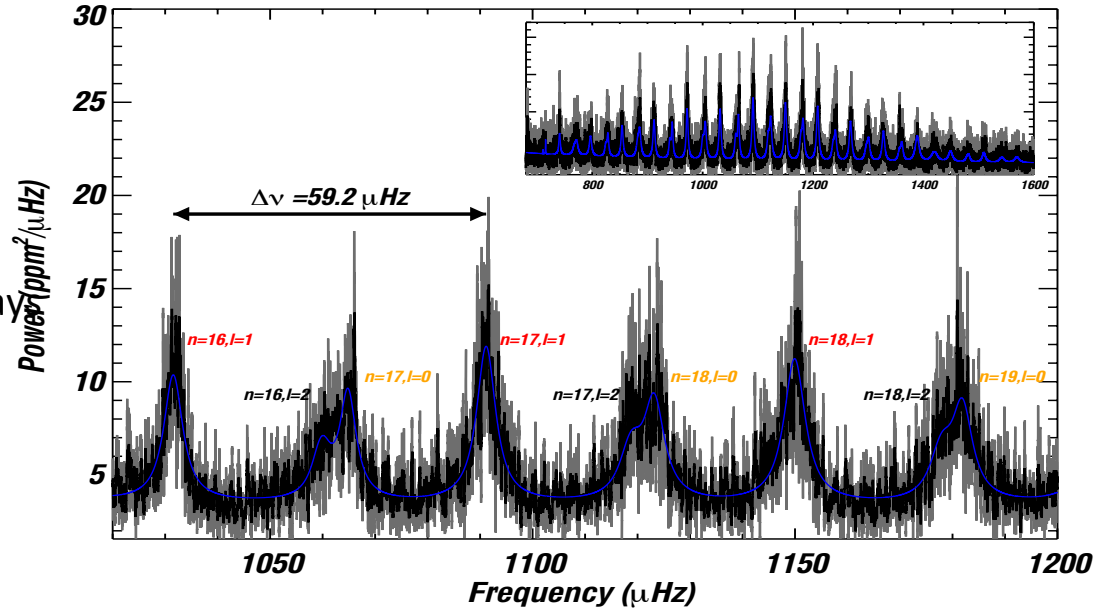
$i_* \sim 30$ degree

Weak constrain on i_* :

Broad modes

Rotation unusually slow for a F-star : ~ 16 days

- ➔ Modes overlap!
- ➔ Hard to disentangle $l=0, 2$
- ➔ Hard to disentangle m -components



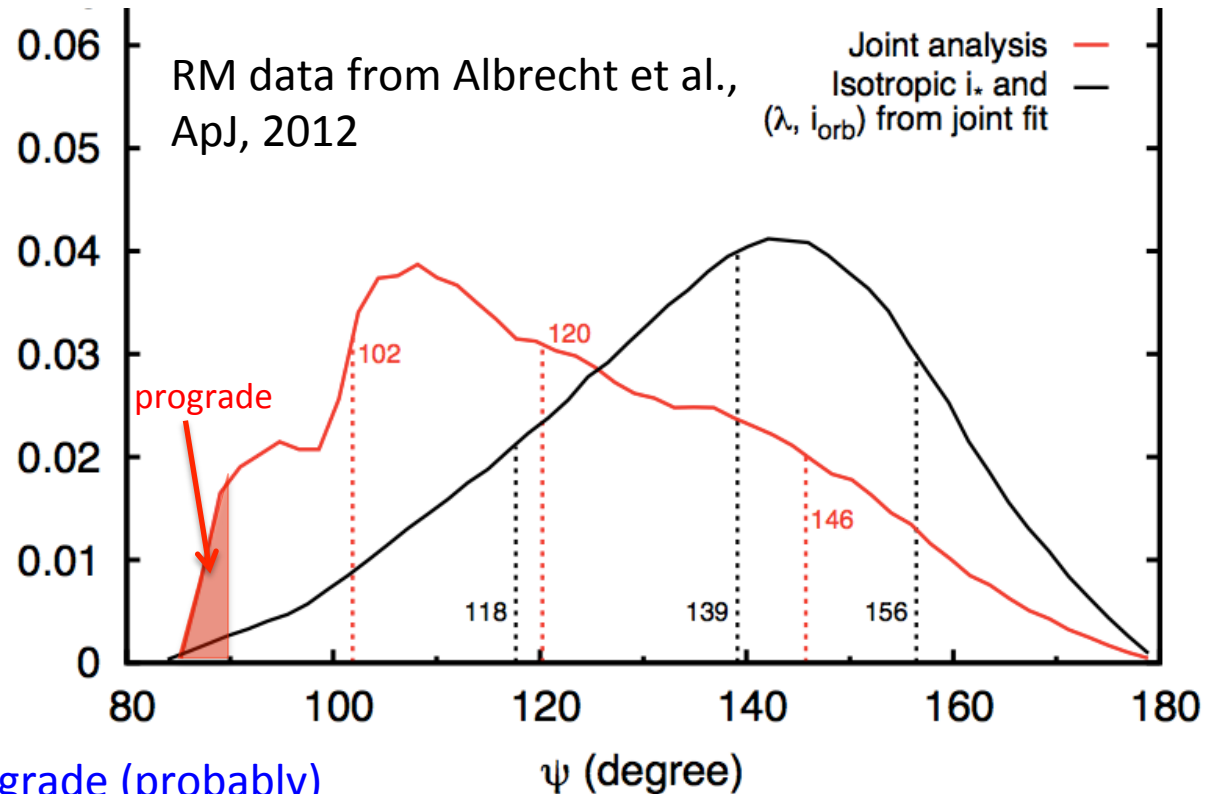
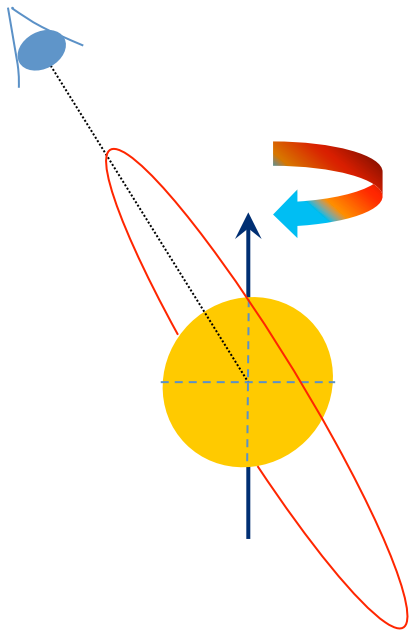
HAT-P-7: a system with a hot Jupiter

$$i_* = 33_{-20}^{+34} \text{ degree}$$

$$\cos i_{\text{orb}} \sim 0.12145(81)$$

$\lambda \sim [157 - 220]$ (depends RM data) degree \rightarrow suggests a oblique, retrograde system

$\psi \sim 120_{-18}^{+26}$ degree \rightarrow quasi-polar orbit



\rightarrow If $|\Psi| > 90$ then the orbit is retrograde (probably)

\rightarrow If $|\Psi| < 90$ then the orbit is prograde (possible)

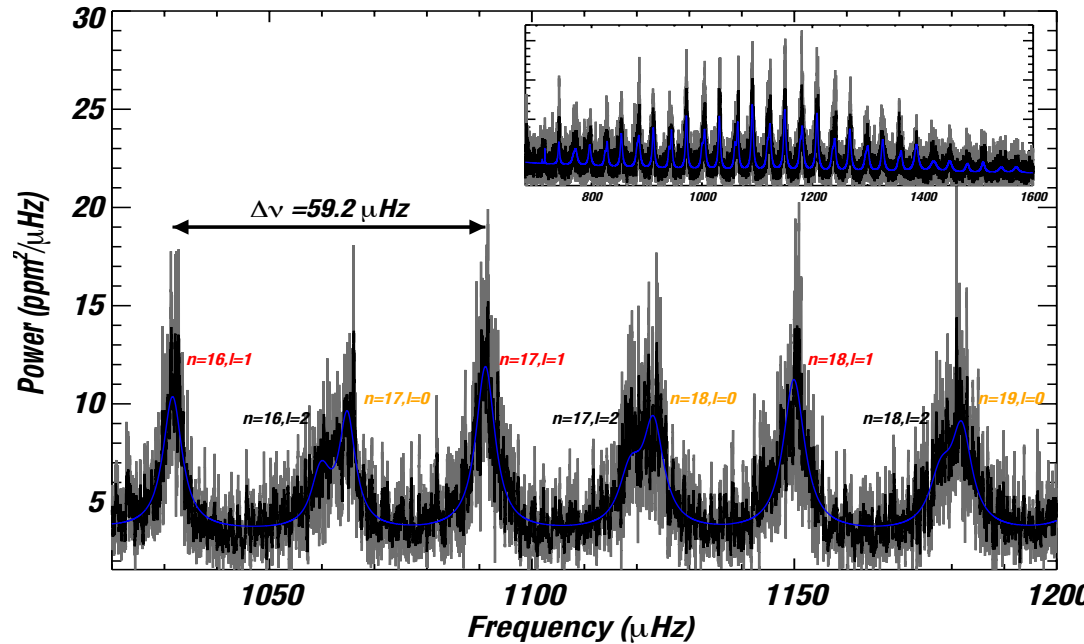
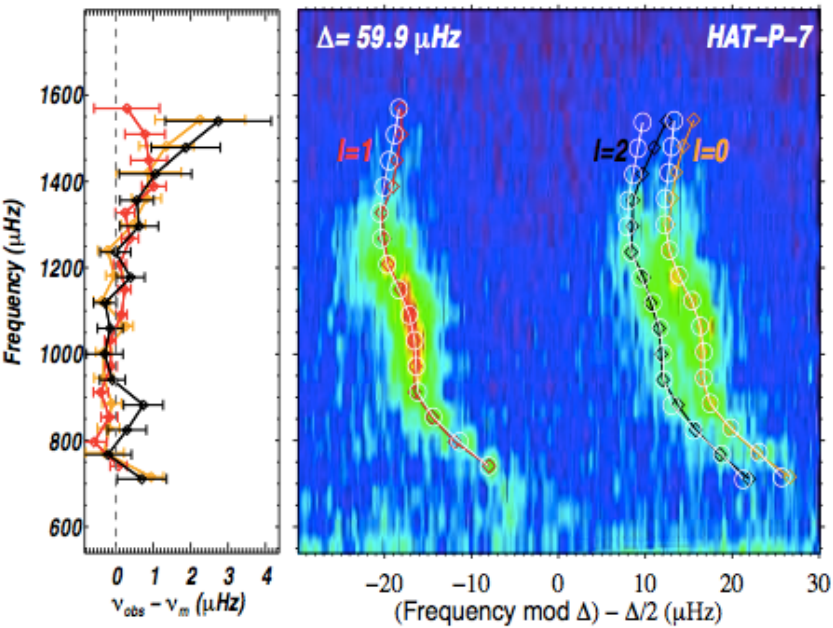
Conclusion

- If for a system we have:
 - The Rossiter McLaughlin effect
 - A transiting planet
 - Solar-like pulsations
- ➔ Measure of the true spin-orbit is possible
- Kepler 25:
 - Is the first system with multiple planets and a MS star to show significant obliquity
 - Only two systems with multiple planets are known to have high obliquities (Huber et al. 2013) ➔ Hard to conclude about the cause of obliquity in multiplanet systems.
- HAT-P-7:
 - Very likely to be on a quasi-polar orbit
 - Likely to be on a retrograde orbit but cannot rule out a prograde orbit

END

Questions?

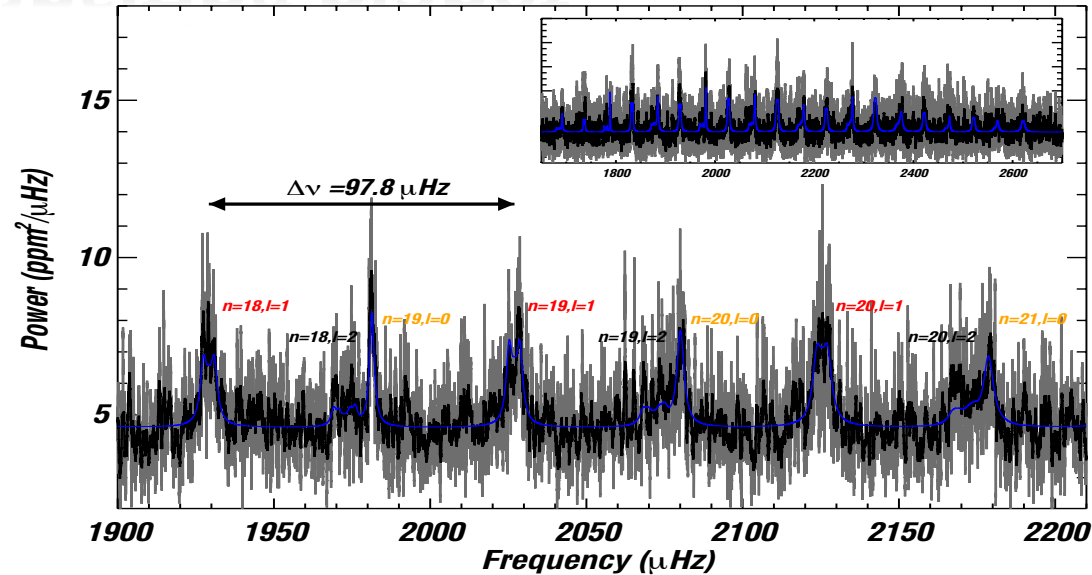
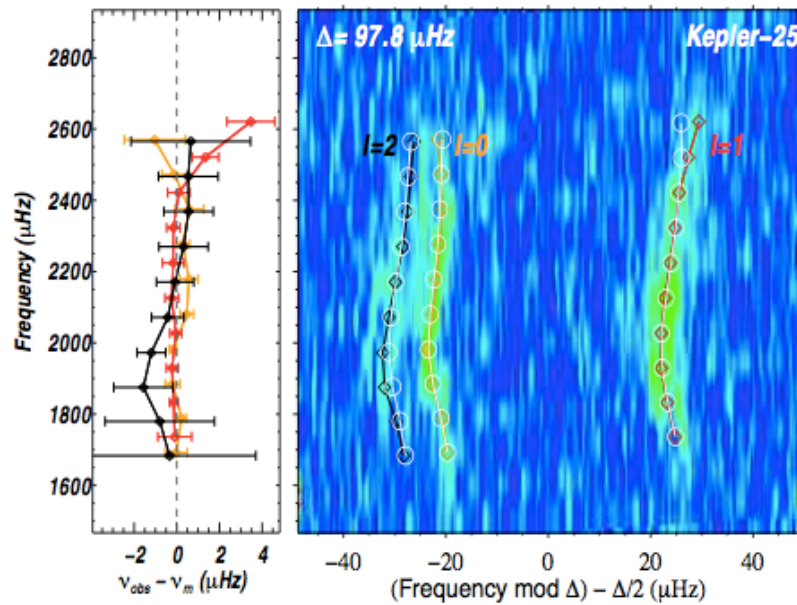
HAT-P-7: a system with a hot Jupiter



parameter	HAT-P-7
M_* (M_\odot)	1.59 ± 0.03
R_* (R_\odot)	2.02 ± 0.01
[Fe/H]	0.32 ± 0.04
T_{eff} (K)	6310 ± 15
Age (Myrs)	1770 ± 100
α_{ov}	$0.000^{+0.002}_{-0.000}$
L/L_\odot	5.84 ± 0.05
$\log g$ (cgs)	4.029 ± 0.002
$\rho_{*,\text{m}}$ (10^3 kg m^{-3})	0.2708 ± 0.0035
$\rho_{*,\text{s}}$ (10^3 kg m^{-3})	0.2696 ± 0.0011
reduced χ^2	1.73

- Modeling with MESA using:
 - Eigenfrequencies (this analysis, Q0-Q16)
 - T_{eff} , [Fe/H], $\log(g)$, L/L_{sun} from Pal et al. (2008)

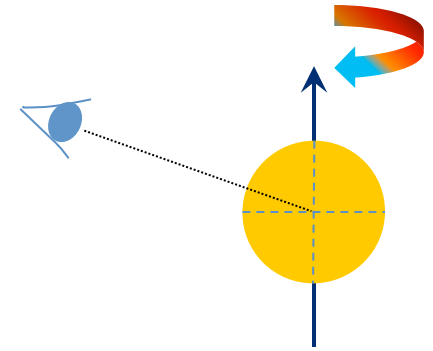
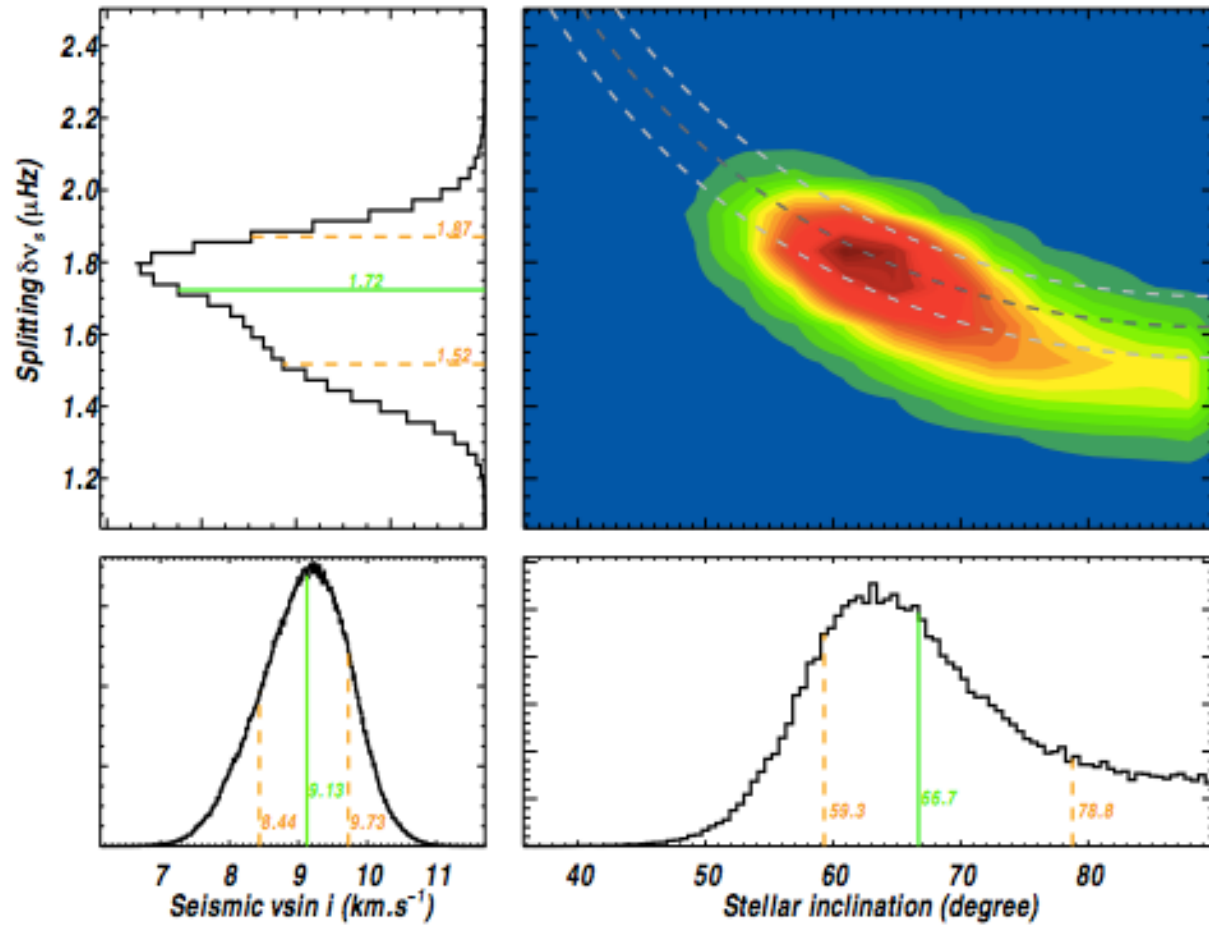
Kepler 25: Two neptunes in transit + one non-transiting planet



parameter	Kepler-25
M_* (M_\odot)	1.26 ± 0.03
R_* (R_\odot)	1.34 ± 0.01
[Fe/H]	0.11 ± 0.03
T_{eff} (K)	6354 ± 27
Age (Myrs)	2750 ± 300
α_{ov}	0.007 ± 0.003
L/L_\odot	2.64 ± 0.07
$\log g$ (cgs)	4.285 ± 0.003
$\rho_{*,m}$ (10^3 kg m^{-3})	0.7367 ± 0.0137
$\rho_{*,s}$ (10^3 kg m^{-3})	0.7356 ± 0.0030
reduced χ^2	1.03

- Modeling with MESA using:
 - Eigenfrequencies (this analysis, Q5-Q16)
 - Teff, [Fe/H], log(g) from Marcy et al. (2014)

Kepler 25: Two neptunes in transit + one non-transiting planet



$i_* \sim 65$ degree

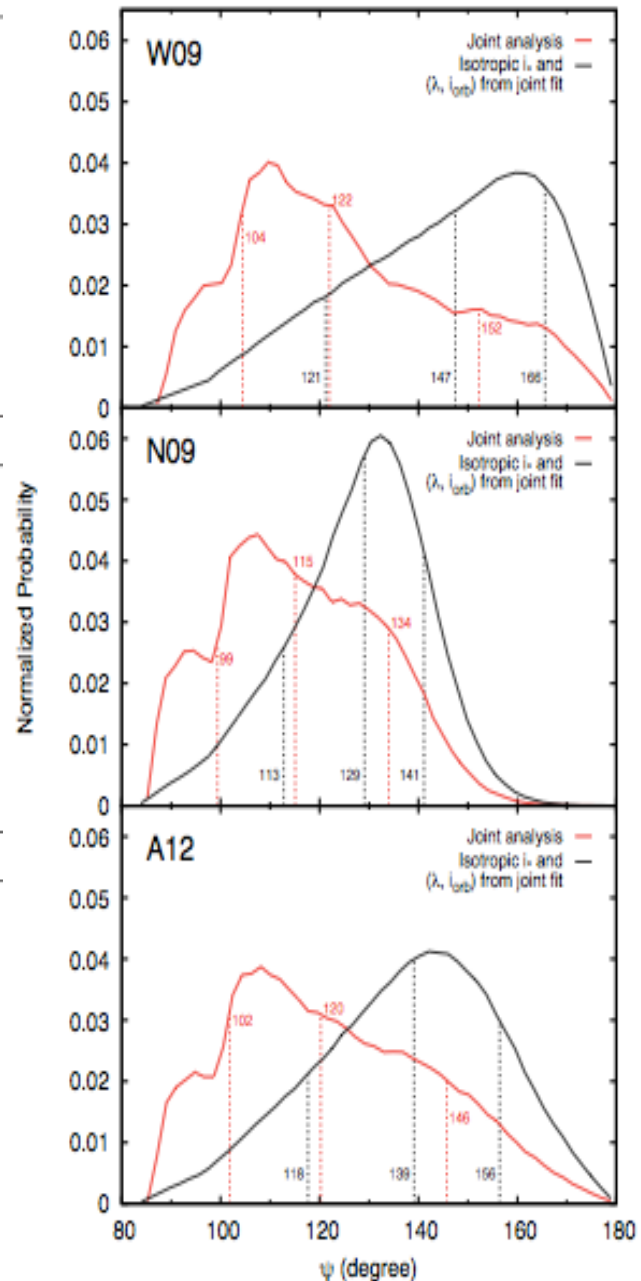
Parameter	Value (W09)	Value (N09)	Value (A12)
<i>Parameters mainly derived from lightcurves (transit, occultation, asteroseismology)</i>			
$t_0(\text{BJD}) - 2454833$		$121.3585049 \pm 0.0000049$	
P (days)		$2.204735427 \pm 0.000000013$	
$e \cos \omega$	0.00024 ± 0.00020	0.00024 ± 0.00020	0.00025 ± 0.00020
$e \sin \omega$	$0.0053^{+0.0022}_{-0.0021}$	$0.0057^{+0.0025}_{-0.0026}$	$0.0049^{+0.0026}_{-0.0030}$
u_1	0.3540 ± 0.0034	$0.3544^{+0.0033}_{-0.0034}$	$0.3545^{+0.0034}_{-0.0035}$
u_2	$0.1670^{+0.0055}_{-0.0054}$	$0.1663^{+0.0055}_{-0.0053}$	$0.1661^{+0.0056}_{-0.0055}$
ρ_* (10^3 kg m^{-3})	0.2736 ± 0.0016	$0.2731^{+0.0021}_{-0.0018}$	$0.2737^{+0.0024}_{-0.0018}$
$\cos i_{\text{orb}}$	$0.12149^{+0.00056}_{-0.00057}$	$0.12166^{+0.00063}_{-0.00068}$	$0.12145^{+0.00061}_{-0.00061}$
R_p/R_*	$0.077589^{+0.000020}_{-0.000021}$	0.077593 ± 0.000020	$0.077591^{+0.000020}_{-0.000021}$
δ		0.01171 ± 0.00010	
$t_{\text{c,tra}}$ (days)		$-0.0000044^{+0.0000041}_{-0.0000042}$	
i_* ($^\circ$)	31^{+33}_{-16}	33^{+34}_{-20}	33^{+34}_{-20}

Parameters mainly derived from RVs

K_* (ms^{-1})	211.7 ± 2.3	213.2 ± 1.8	214.0 ± 4.6
γ_1 (ms^{-1})	-15.5 ± 3.0	-37.5 ± 1.5	$10.4^{+1.5}_{-1.6}$
γ_2 (ms^{-1})	-9.7 ± 1.7	-16.9 ± 1.4	-
$\dot{\gamma}$ ($\text{ms}^{-1} \text{ yr}^{-1}$)	21.5 ± 2.5	-	-
λ ($^\circ$)	186^{+10}_{-11}	$220.3^{+8.2}_{-9.3}$	157^{+14}_{-13}
$v \sin i_*$ (kms^{-1})	$4.15^{+0.38}_{-0.39}$	3.17 ± 0.33	$3.17^{+0.33}_{-0.34}$
β (kms^{-1})		3.0 (fixed)	
γ (kms^{-1})		1.0 (fixed)	
ζ (kms^{-1})	5.3 ± 1.5	5.5 ± 1.5	5.5 ± 1.5
$u_{1\text{RM}} + u_{2\text{RM}}$		0.70 ± 0.10	
$u_{1\text{RM}} - u_{2\text{RM}}$		-0.23 (fixed)	

Derived quantities

ψ ($^\circ$)	122^{+30}_{-18}	115^{+19}_{-16}	120^{+26}_{-18}
a/R_*	$4.1269^{+0.0082}_{-0.0078}$	$4.1245^{+0.0103}_{-0.0092}$	$4.1277^{+0.0121}_{-0.0090}$
transit impact parameter (R_*)	0.4987 ± 0.0013	0.4989 ± 0.0013	$0.4988^{+0.0013}_{-0.0014}$
$T_{14,\text{tra}}$ (days)	0.164301 ± 0.000022	0.164303 ± 0.000023	0.164300 ± 0.000023
$T_{23,\text{tra}}$ (days)	$0.133042^{+0.000049}_{-0.000048}$	$0.133034^{+0.000047}_{-0.000048}$	$0.133037^{+0.000052}_{-0.000048}$
T_{tra} (days)	$0.148672^{+0.000025}_{-0.000024}$	0.148668 ± 0.000024	$0.148669^{+0.000025}_{-0.000024}$
occultation impact parameter (R_*)	$0.5040^{+0.0022}_{-0.0023}$	$0.5047^{+0.0025}_{-0.0028}$	$0.5039^{+0.0024}_{-0.0033}$
$T_{14,\text{occ}}$ (days)	$0.16555^{+0.00051}_{-0.00050}$	$0.16566^{+0.00058}_{-0.00061}$	$0.16547^{+0.00060}_{-0.00070}$
$T_{23,\text{occ}}$ (days)	$0.13385^{+0.00034}_{-0.00033}$	$0.13392^{+0.00039}_{-0.00040}$	$0.13379^{+0.00041}_{-0.00046}$
T_{occ} (days)	$0.14970^{+0.00042}_{-0.00041}$	$0.14979^{+0.00048}_{-0.00051}$	$0.14963^{+0.00050}_{-0.00058}$
occultation depth (ppm)		70.5 ± 0.6	
$M_p(M_J)$	1.86 ± 0.03	1.87 ± 0.03	1.88 ± 0.05
$R_p(R_J)$		1.526 ± 0.008	
ρ_p (10^3 kg m^{-3})	0.65 ± 0.01	0.66 ± 0.01	0.66 ± 0.02



Parameter	Value (A13)
<i>Parameters mainly derived from lightcurves (transit, asteroseismology)</i>	
$t_0(\text{BJD}) - 2454833$	$127.646558^{+0.000096}_{-0.000094}$
P (days)	$12.7203724^{+0.0000014}_{-0.0000013}$
$u_1 + u_2$	0.550 ± 0.018
$u_1 - u_2$	-0.27 ± 0.44
ρ_* (10^3 kg m^{-3})	$0.733^{+0.013}_{-0.012}$
$\cos i_{\text{orb}}$	$0.04788^{+0.00036}_{-0.00038}$
R_p/R_*	$0.03590^{+0.00054}_{-0.00046}$
i_* ($^\circ$)	$65.4^{+10.6}_{-6.4}$
<i>Parameters mainly derived from RVs</i>	
$K_{*,2011}$ (ms^{-1})	-13 ± 22
$K_{*,2012}$ (ms^{-1})	-37 ± 30
γ_{2011} (ms^{-1})	-3.5 ± 1.3
γ_{2012} (ms^{-1})	2.0 ± 1.4
λ ($^\circ$)	9.4 ± 7.1
$v \sin i_*$ (kms^{-1})	$9.34^{+0.37}_{-0.39}$
β (kms^{-1})	3.0 (fixed)
γ (kms^{-1})	1.0 (fixed)
ζ (kms^{-1})	4.9 ± 1.5
$u_{1\text{RM}} + u_{2\text{RM}}$	0.69 ± 0.10
$u_{1\text{RM}} - u_{2\text{RM}}$	-0.0297 (fixed)
<i>Derived quantities</i>	
ψ ($^\circ$)	$26.9^{+7.0}_{-9.2}$
a/R_*	18.44 ± 0.11
transit impact parameter (R_*)	0.8826 ± 0.0018
$T_{14,\text{tra}}$ (days)	0.11925 ± 0.00025
$T_{23,\text{tra}}$ (days)	$0.08528^{+0.00065}_{-0.00069}$
T_{tra} (days)	$0.10226^{+0.00036}_{-0.00037}$

